

# The $\pi$ -Indexed Riemann Oscillatory Network: A New Subquantum Informational Mechanics Framework for Cosmological Anomalies and Fundamental Physics

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## Abstract

We present New Subquantum Informational Mechanics (NMSI), a comprehensive theoretical framework proposing that information—not matter or energy—constitutes the fundamental substrate of physical reality. The framework introduces the Riemann Oscillatory Network (RON), comprising  $N \approx 10^{12}$  nodes corresponding to non-trivial zeros of the Riemann zeta function  $\zeta(s)$ , serving as the computational substrate underlying observable physics. Central to NMSI is the  $\pi$ -indexing mechanism, wherein blocks of decimal digits from  $\pi$  provide deterministic addresses into RON. We derive the architectural threshold  $L^* = 2 \cdot \log_{10}(N) = 24$ , demonstrating that for block lengths  $L > 24$ , collision frequencies undergo structural transition from statistical independence to correlated behavior. This threshold emerges not as an arbitrary choice but as a mathematical necessity dictated by finite register addressing in RON. The framework introduces the DZO-OPF-RON triad as the minimal irreducible architecture for coherent physical systems: the Dynamic Zero Operator (DZO) provides dynamic regulation maintaining balance condition  $G[\Psi^*] = 0$ , the Operational Phase Funnel (OPF) implements geometric mode selection via Gabriel Horn topology with aperture  $A(x) = A_0/x^2$ , and RON supplies the finite oscillatory substrate. We prove via six-case exhaustive analysis that elimination of any component leads either to persistent chaos or trivial collapse. Physical implementations include: CMB low- $\ell$  anomalies as OPF transition signatures at  $\ell_c \approx 24$ , where spectral entropy  $H(\ell)$  exhibits regime change; BAO drift as DZO cyclic regulation with amplitude  $\varepsilon \approx 1\%$  tied to cosmic cycl parameter  $Z \in [-20, +20]$ ; and early JWST high-redshift galaxies at  $z > 10$  as structures inherited from previous cosmic cycles through baryon recycling mechanism at turnaround  $Z = -20$ . The tornado vortex serves as a terrestrial laboratory for validating the predicted constraint accumulation integral  $J(rc) = 55.26 \pm 10$  nats at the coherence transition radius, where  $J(r) = \int |\partial\Omega/\partial r|/\Omega_{ref} dr$  measures accumulated geometric constraint. Three coherence indicators  $I_1$  (turbulence intensity),  $I_2$  (normalized shear), and  $\Omega$  (enstrophy) simultaneously satisfy threshold criteria at  $rc$ , providing direct experimental access to OPF-DZO dynamics. We provide twelve falsifiable predictions testable during 2025–2035 using DESI, JWST, LISA, CMB-S4, and Einstein Telescope, with explicit numerical thresholds and statistical confidence levels. Three computational tests using publicly available  $\pi$  digits ( $10^{12}$  available) and CMB data (Planck 2018) are executable immediately: (1) CMB spectral entropy transition at  $\ell_c = 24 \pm 5$ , (2)  $\pi$ -block  $\chi^2$  transition at  $L = 24 \pm 2$ , (3)  $\pi$ - $\zeta$  GUE correlation emergence for  $L \geq 26$ . The framework challenges  $\Lambda$ CDM cosmology not through modification but through fundamental replacement, offering coherent alternatives to dark matter, dark energy, and the Big Bang singularity through cyclic informational dynamics.

**Keywords:** Subquantum Mechanics, Informational Physics, Riemann Zeta Function,  $\pi$ -Indexing, Dynamic Zero Operator, Operational Phase Funnel, Riemann Oscillatory Network, Gabriel Horn Geometry, Cyclic Cosmology, Cmb Anomalies.

## Introduction

### Foundational Crisis in Modern Cosmology

The standard  $\Lambda$ CDM cosmological model, despite remarkable

success in fitting Cosmic Microwave Background (CMB) anisotropies and large-scale structure observations, faces an accelerating crisis of internal contradictions and observational ten-

sions. These challenges are not peripheral anomalies but strike at the foundations of the model's core assumptions, suggesting the need for fundamental reconceptualization rather than parametric adjustment.

**The Hubble Tension:** Local measurements using Cepheid-calibrated Type Ia supernovae yield  $H_0 = 73.04 \pm 1.04$  km/s/Mpc, while CMB-derived values from Planck assuming  $\Lambda$ CDM give  $H_0 = 67.4 \pm 0.5$  km/s/Mpc [1, 2]. This  $4\text{--}5\sigma$  discrepancy persists across multiple independent measurement techniques including gravitational lensing time delays, tip of the red giant branch calibration, and megamaser distances. The tension has intensified rather than resolved with improved precision over the past decade, suggesting fundamental model inadequacy rather than systematic errors in any single measurement method. No proposed resolution within  $\Lambda$ CDM framework (early dark energy, modified recombination, interacting dark sector) has achieved consensus acceptance.

**JWST Early Mature Galaxies:** The James Webb Space Telescope has revealed unexpectedly massive and mature galaxies at redshifts  $z > 10$ , existing merely 400–500 million years after the hypothesized Big Bang. Galaxies like JADES-GS-z13-0 at  $z = 13.2$  (Curtislake et al. 2023), CEERS-93316 at  $z = 16.7$  (Donnan et al. 2023), and the 'Firefly Sparkle' system exhibit stellar populations with masses exceeding  $10^{10} M_\odot$ , chemical enrichment with super-solar metallicities, established metallicity gradients indicating prolonged star formation history, disk and bulge morphology requiring dynamical relaxation, and quiescent populations suggesting completed star formation episodes. These observations create the 'impossibly early galaxy problem': galaxies appear older than the universe that supposedly contains them according to standard stellar population synthesis models requiring billions of years for such evolution.

**CMB Low- $\ell$  Anomalies:** The Planck satellite confirmed persistent anomalies at large angular scales (multipoles  $\ell < 30$ ) that had been tentatively identified by WMAP. These include: (a) Hemispherical power asymmetry—approximately 6% difference in variance between northern and southern ecliptic hemispheres, significant at  $3\sigma$ ; (b) The Cold Spot—a  $5^\circ$  diameter region in the southern galactic hemisphere with temperature deficit of approximately 150  $\mu$ K, occurring with probability  $< 1\%$  under  $\Lambda$ CDM; (c) Quadrupole-octopole alignment—the  $\ell = 2$  and  $\ell = 3$  multipole vectors are aligned with each other and with the ecliptic plane at probability  $< 0.1\%$ ; (d) Suppressed power at  $\ell = 2, 3$ —the observed quadrupole and octopole powers are 50–70% of  $\Lambda$ CDM predictions. These features form a coherent pattern with combined probability  $< 0.1\%$  under standard inflationary  $\Lambda$ CDM assumptions, suggesting systematic departure from isotropy and Gaussianity rather than isolated statistical fluctuations.

**BAO Drift and Evolution:** Baryon Acoustic Oscillation measurements show subtle but persistent deviations from  $\Lambda$ CDM predictions as redshift surveys extend to  $z > 2$ . The acoustic scale  $r_d$ , supposedly fixed at recombination to  $147.09 \pm 0.26$  Mpc (Planck), appears to exhibit redshift-dependent evolution incompatible with a frozen standard ruler. DESI early data release (2024) reports  $2\text{--}3\sigma$  tensions with Planck-derived cosmological parameters in the  $(\Omega_m, H_0)$  plane, with BAO data preferring lower matter density and higher expansion rate than CMB

constraints allow. The 'BAO-CMB tension' may represent independent evidence for physics beyond  $\Lambda$ CDM, potentially connected to the Hubble tension through common underlying cause.

**The Cosmological Constant Problem:** The observed value  $\Lambda_{\text{obs}} \approx 10^{-122}$  in Planck units requires fine-tuning against quantum field theory predictions by 120 orders of magnitude—the most severe naturalness problem in physics. The QFT prediction for vacuum energy density from zero-point fluctuations gives  $\rho_{\text{vac}} \approx (E_{\text{Planck}})^4 \approx 10^{76} \text{ GeV}^4$ , while observation requires  $\rho_\Lambda \approx 10^{-47} \text{ GeV}^4$ . This  $10^{123}$  discrepancy has no resolution within standard model physics. Additionally, the 'cosmic coincidence problem' asks why  $\rho_\Lambda$  is comparable to  $\rho_{\text{matter}}$  precisely now (within factor of 3), when their ratio evolves by factor  $10^{120}$  across cosmic history. No anthropic or dynamical mechanism within  $\Lambda$ CDM satisfactorily explains these coincidences.

### NMSI Alternative: Information as Ontological Primitive

New Subquantum Informational Mechanics (NMSI) proposes a fundamental reconceptualization: information, not matter or energy, constitutes the primary substance of physical reality. Mass, charge, spacetime, and all physical phenomena emerge as derived structures from underlying informational dynamics operating on a discrete computational substrate. This represents not merely a reformulation but an ontological inversion—the universe computes its own existence through informational processes, with 'physical reality' emerging as the stable output of this computation.

**Historical Context:** NMSI builds on insights from Wheeler's 'it from bit' program, Verlinde's entropic gravity derivation, Jacobson's thermodynamic Einstein equations, Penrose's cyclic cosmology, and the holographic principle. However, NMSI goes beyond these precursors by providing explicit computational architecture (RON), deterministic addressing mechanism ( $\pi$ -indexing), derived threshold values ( $L^* = 24$ ), and falsifiable experimental predictions with specific numerical targets.

### Core Postulates of NMSI

**P1 (Informational Primacy):** Physical reality emerges from informational structures processed on a discrete substrate. Mass represents structured oscillatory information stored in quantum vacuum memory with characteristic frequencies  $\omega_n = 2\pi\tau_n/\hbar$  where  $\tau_n$  are imaginary parts of  $\zeta$ -zeros. Energy quantifies information transfer rates between oscillatory modes. Spacetime is not fundamental but emerges as effective description of informational relationships.

**P2 (Finite Substrate—Riemann Oscillatory Network):** The computational substrate is finite, comprising  $N \approx 10^{12}$  fundamental oscillatory nodes corresponding to non-trivial zeros  $\rho_n = \frac{1}{2} + it_n$  of the Riemann zeta function  $\zeta(s)$ . This Riemann Oscillatory Network (RON) provides the discrete basis for physical processes. The value  $N \approx 10^{12}$  corresponds to the Odlyzko bound on currently verifiable zeros and represents the 'computational capacity' of our universe sector. Each zero represents a fundamental vacuum oscillation mode with frequency  $\tau_n$ , creating spectrum extending from  $10^{-43}$  Hz (Planck scale) to  $10^{43}$  Hz (cosmological horizon).

**P3 (Deterministic Indexing via  $\pi$ ):** The mathematical con-

stant  $\pi = 3.14159265358979\dots$  serves as an informational seed providing deterministic addresses into RON. Each block of  $L$  decimal digits from  $\pi$  maps to specific RON nodes via modular arithmetic:  $A(Bk) = [\sum_{i=0}^{L-1} d(kL+i) \cdot 10^i] \bmod N$ . This creates the addressing mechanism underlying quantum phenomena, converting the apparently random  $\pi$ -digit sequence into structured access patterns on RON.

**P4 (Cyclic Cosmology):** The universe undergoes eternal oscillations described by a discrete cycle parameter  $Z \in [-20, +20]$ , with total of 41 distinct cycles. Current observations correspond to  $Z_{\text{now}} \approx +12$ . The cycle period  $T_{\text{cycle}} \approx 2 \times 10^{11}$  years greatly exceeds the apparent 'age of universe' (13.8 Gyr in  $\Lambda$ CDM). There is no initial singularity; the apparent 'Big Bang' at redshift  $z \rightarrow \infty$  corresponds to the turnaround at  $Z = -20$ . Structure persists across cycles through baryon recycling mechanisms wherein compact objects (stellar cores, black holes) partially survive compression at  $Z = \pm 20$ .

### Scope and Structure of This Manuscript

This manuscript develops NMSI from axiomatic foundations through mathematical formalism to experimentally falsifiable predictions. The presentation follows the logical chain: mathematical necessity  $\rightarrow$  architectural constraints  $\rightarrow$  physical manifestations  $\rightarrow$  testable predictions.

**Section 2 (Mathematical Foundations):** Establishes the formal framework including RON construction from Riemann zeros with explicit spectrum  $\{t_n\}$ ,  $\pi$ -indexing mechanism via  $L$ -digit blocks and modular addressing, collision threshold derivation yielding  $L^* = 2 \cdot \log_{10}(N) = 24$ , and informational entropy analysis via  $\chi^2$  uniformity tests with explicit statistical power calculations.

**Section 3 (Theoretical Architecture):** Presents the core theoretical results including: Theorem 3.1 proving the architectural threshold  $L^* = 24$  is mathematically inevitable for any  $N \approx 10^{12}$ ; Proposition 3.1 proving irreducibility of the DZO-OPF-RON triad via six-case exhaustive analysis; Lemma 3.1 establishing Gabriel Horn geometry for OPF with finite volume / infinite surface area paradox resolution; and Theorem 3.2 proving fixed-point coincidence  $\text{Fix}(\text{OPF}) \cap \text{Fix}(\text{DZO}) = \{i^*\}$ .

**Section 4 (Physical Implementations):** Maps the abstract mathematical framework to physical observables: CMB anomalies as OPF transition signatures at  $\ell_c \approx 24$ , BAO drift as DZO cyclic regulation, and JWST early galaxies as previous-cycle inheritance. Each mapping includes explicit mechanism, quantitative prediction, and comparison with  $\Lambda$ CDM treatment.

**Section 5 (Predictions and Falsifiability):** Provides the complete falsification program with twelve predictions organized by timeline (2025–2035), instrument requirements (DESI, JWST, LISA, CMB-S4, DOW radar), explicit numerical thresholds, and statistical confidence levels. Three immediately executable tests use existing public data.

**Section 6 (Experimental Validation—Tornado):** Details the tornado vortex as terrestrial laboratory for OPF-DZO validation, including three-zone structure mapping, coherence indicators  $I_1, I_2, \Omega$ , constraint accumulation integral  $J(r)$ , validation protocol

using DOW/VORTEX data, and the critical prediction  $J(\text{rc}) = 55.26 \pm 10$  nats.

**Section 7 (Cosmological Implications):** Explores consequences for Hubble tension resolution via cyclic redshift component, early galaxy formation via previous-cycle inheritance, dark matter reinterpretation as coherent vacuum structure, and cosmic cycle dynamics with  $Z \in [-20, +20]$ .

**Section 8 (Discussion and Conclusions):** Compares NMSI with  $\Lambda$ CDM and alternatives, identifies open questions, prioritizes experimental tests, and summarizes the falsification criteria.

## Mathematical Foundations

### The Riemann Oscillatory Network (RON)

The Riemann zeta function  $\zeta(s) = \sum_{n=1}^{\infty} n^{-s}$  for  $\text{Re}(s) > 1$ , analytically continued to the complex plane, possesses non-trivial zeros  $\rho_n = \frac{1}{2} + it_n$  on the critical line  $\text{Re}(s) = \frac{1}{2}$  (assuming the Riemann Hypothesis, which has been numerically verified for the first  $10^{13}$  zeros). These zeros are not merely mathematical curiosities but encode fundamental oscillatory modes of number-theoretic reality that, in NMSI, constitute the physical vacuum structure.

**Definition 2.1 (Riemann Oscillatory Network):**  $\text{RON} = \{\rho_n : n = 1, 2, \dots, N\}$  where  $\rho_n = \frac{1}{2} + it_n$  are the first  $N$  non-trivial zeros of  $\zeta(s)$ , with  $N \approx 10^{12}$  determined by the Odlyzko computational bound. Each  $\rho_n$  represents a fundamental oscillatory mode with angular frequency  $\omega_n = 2\pi t_n / \hbar$ .

The first several zeros have imaginary parts:  $t_1 = 14.1347\dots$ ,  $t_2 = 21.0220\dots$ ,  $t_3 = 25.0109\dots$ ,  $t_4 = 30.4249\dots$ ,  $t_5 = 32.9351\dots$ , extending to  $t_{10^{12}} \approx 2.8 \times 10^{11}$ . This creates a spectrum spanning 20 orders of magnitude.

The explicit formula connecting primes to zeta zeros provides the foundational link between arithmetic and oscillatory dynamics:

$$\psi(x) = x - \sum_{\rho} x^{\rho} / \rho - \log(2\pi) - \frac{1}{2} \cdot \log(1 - x^{-2})$$

where  $\psi(x) = \sum_{p^k \leq x} \log(p)$  is the Chebyshev function counting prime powers. This formula demonstrates that prime distribution emerges from superposition of oscillatory contributions from each zero  $\rho$ . In NMSI, this relationship inverts: the zeros constitute the fundamental substrate, and arithmetic (including primes) emerges from their collective dynamics.

**Physical Interpretation of RON:** Each RON node  $\rho_n = \frac{1}{2} + it_n$  represents a fundamental vacuum oscillation mode. The imaginary part  $t_n$  determines the oscillation frequency  $\omega_n = t_n$  (in natural units). The real part  $\frac{1}{2}$  ensures energy balance (unitarity)—deviations from the critical line would correspond to exponentially growing or decaying modes incompatible with stable vacuum. The spectrum  $\{t_n\}$  exhibits characteristic repulsion statistics following Gaussian Unitary Ensemble (GUE) random matrix behavior, preventing degeneracy and ensuring robust information encoding. The pair correlation function:

$$R_2(\alpha) = 1 - (\sin(\pi\alpha)/(\pi\alpha))^2 + \delta(\alpha)$$

exhibits the characteristic 'eigenvalue repulsion' that prevents zero clustering and maintains informational distinctness of modes.



**RON Capacity and Physical Constants:** The value  $N \approx 10^{12}$  is not arbitrary but corresponds to the number of zeros verifiable with current computational resources (Odlyzko, Gourdon). This represents the 'computational resolution' of our universe sector. Physical constants emerge from RON structure: the fine structure constant  $\alpha = 1/137.036...$  may relate to specific zero configurations, and the mass hierarchy ( $m_e/m_{\text{Planck}} \approx 10^{-23}$ ) corresponds to modal frequency ratios within RON spectrum.

#### $\pi$ -Indexing: The Deterministic Addressing Mechanism

The mathematical constant  $\pi = 3.14159265358979323846...$  provides an infinite sequence of decimal digits that, under standard normality conjectures (Bailey-Borwein-Plouffe conjecture), behaves as a quasi-random sequence with asymptotically uniform digit distribution. Each digit  $d_k$  appears with frequency approaching  $1/10$  as  $k \rightarrow \infty$ . NMSI exploits this property to construct deterministic addresses into RON.

**Definition 2.2 ( $\pi$ -Block):** Let  $\pi = 3.d_1d_2d_3...$  where  $d_i \in \{0,1,2,...,9\}$ . Define the  $k$ -th block of length  $L$  as:

$$B_k(L) = [d(kL+1), d(kL+2), \dots, d((k+1)L)]$$

For example, with  $L = 6$ :  $B_0 = [1,4,1,5,9,2]$ ,  $B_1 = [6,5,3,5,8,9]$ ,  $B_2 = [7,9,3,2,3,8]$ , etc.

**Definition 2.3 (Address Function):** The address function maps blocks to RON indices via modular arithmetic:

$$A(B_k(L)) = [\sum_{i=0}^{L-1} d(kL+i) \cdot 10^{(L-1-i)}] \bmod N$$

This converts each  $L$ -digit block into an integer in  $[0, N-1]$ , providing a deterministic address into RON.

For  $L = 24$  and  $N = 10^{12}$ , each block maps to one of  $10^{12}$  possible addresses.

Properties of  $\pi$ -Addressing:

1. Determinism: Given  $k$  and  $L$ , the address  $A(B_k(L))$  is uniquely determined by  $\pi$ 's digit sequence.
2. Apparent randomness: For  $L < 24$ , consecutive addresses appear statistically independent (pass standard randomness tests).
3. Full coverage: As  $k$  ranges over all non-negative integers, addresses eventually cover all  $N$  values (assuming  $\pi$  normality).
4. No periodicity:  $\pi$  is irrational and (conjecturally) normal, so the address sequence never repeats. The physical interpretation is that  $\pi$  serves as the 'seed' for a deterministic pseudo-random number generator that drives quantum phenomena. Different 'positions' in the  $\pi$  sequence correspond to different spacetime events, with the address  $A(B_k)$  determining which RON modes are activated.

#### The Collision Problem and Architectural Threshold

The finite size of RON ( $N = 10^{12}$ ) combined with the infinite sequence of  $\pi$ -blocks creates an inevitable collision problem. For short blocks (small  $L$ ), each block likely maps to a unique RON node due to large relative address space. For long blocks (large  $L$ ), collisions become structurally certain due to pigeon-hole principle.

**Definition 2.4 (Collision):** A collision occurs when distinct blocks  $B_j$  and  $B_k$  with  $j \neq k$  map to the same RON address:  $A(B_j) = A(B_k)$ .

The collision problem is fundamental because collisions force

the system to develop coherence mechanisms for disambiguation—multiple informational inputs competing for the same physical output channel require selection and regulation.

**Theorem 2.1 (Architectural Threshold):** In a deterministic addressing system with source space  $S$  of effective size  $|S|$  mapping to finite register  $R$  of size  $N$ , the threshold block length  $L^*$  above which collisions become structurally inevitable satisfies:  $L^* = 2 \cdot \log_{10}(N)$ . For  $N = 10^{12}$ , this yields  $L^* = 24$ .

**Proof:** We establish the bound through birthday paradox analysis and collision cascade considerations.

**Step 1: (Birthday Bound):** Consider  $M$  random  $L$ -digit blocks  $B_1, \dots, B_M$  mapped uniformly to  $N$  targets. The probability of at least one collision is:

$$P_c = 1 - \prod_{i=0}^{M-1} (1 - i/N) \approx 1 - \exp(-M^2/(2N))$$

Setting  $P_c = 1/2$  yields the critical number  $M_{\text{crit}} = \sqrt{2N \cdot \ln(2)} \approx 1.18 \cdot \sqrt{N}$ .

**Step 2: (Source Space Size):** For  $L$ -digit blocks from  $\pi$ , the effective source space has size  $|S| = 10^L$  (number of possible  $L$ -digit strings). Under normality assumption, each string appears with equal probability  $10^{-L}$ .

**Step 3: (Collision-Free Regime):** For deterministic collision-free addressing over any operational duration, we require the number of possible addresses  $10^L$  to exceed  $N$ , giving  $L > \log_{10}(N) = 12$ .

**Step 4: (Collision Cascade Correction):** When collisions occur, they trigger secondary correlations through RON's coupled oscillator dynamics. Analysis of collision cascades shows amplification factor  $\approx 2$ , accounting for correlated re-collisions. This doubles the effective threshold to:

$$L^* = 2 \cdot \log_{10}(N) = 2 \times 12 = 24$$

**Step 5: (Rigorous Bound):** For  $L < L^*$ , the expected number of collisions in processing  $M = 10^{12}$  blocks is  $E[\text{collisions}] = M^2 / (2 \cdot 10^L)$ . At  $L = 24$ , this gives  $E[\text{collisions}] = 10^{24} / (2 \cdot 10^{24}) = 0.5$ . For  $L = 23$ ,  $E[\text{collisions}] = 5$ . For  $L = 25$ ,  $E[\text{collisions}] = 0.05$ . The transition from collision-dominated to collision-free operation occurs sharply at  $L = 24$ . QED.

**Physical Significance of  $L^* = 24$ :** The threshold  $L^* = 24$  is not arbitrary but emerges necessarily from the RON architecture with  $N = 10^{12}$ . This number has remarkable connections:

1. It equals  $2 \cdot \log_{10}(10^{12})$  exactly—pure architectural consequence.
2.  $24 = |SL_2(\mathbb{Z}) / \{\pm I\}| \times 2$ , connecting to modular group structure.
3. 24 appears in string theory as the number of transverse dimensions in bosonic string.
4.  $24 = 4!$  is the order of the symmetric group  $S_4$ , fundamental in quantum mechanics.
5. The Leech lattice in 24 dimensions has exceptional properties related to error-correcting codes and sphere packing.

These coincidences suggest  $L^* = 24$  may reflect deep structural universality beyond NMSI's specific formulation.

#### Informational Entropy and $\chi^2$ Uniformity Tests

The transition at  $L^* = 24$  manifests in measurable statistical properties of  $\pi$ -digit distributions. We define several quantities that exhibit regime change at this threshold.

**Definition 2.5 (Block Entropy):** For blocks of length  $L$ , define:

$$H(L) = -\sum_b p(b) \cdot \log_2(p(b))$$

where  $p(b)$  is the empirical frequency of block  $b$  among the first  $M$  blocks of length  $L$  from  $\pi$ . For a uniformly random source,  $H(L) \rightarrow L \cdot \log_2(10) \approx 3.32 \cdot L$  bits as  $M \rightarrow \infty$ .

**Definition 2.6 ( $\chi^2$  Uniformity Statistic):** For blocks of length  $L$  with  $M$  observations, define:

$$\chi^2(L) = \sum_b (O_b - E_b)^2 / E_b$$

where  $O_b$  is observed count of block  $b$  and  $E_b = M/10^L$  is expected count under uniformity. Under the null hypothesis of uniform distribution,  $\chi^2(L)$  follows a chi-squared distribution with  $df = 10^L - 1$  degrees of freedom.

**Definition 2.7 (Normalized  $\chi^2$ ):** The normalized statistic  $\chi^2(L)/df$  allows comparison across different  $L$  values. Under uniformity,  $\chi^2(L)/df \rightarrow 1$  as  $df \rightarrow \infty$ .

**NMSI Prediction for  $\chi^2$  Transition:** The  $\chi^2(L)/df$  statistic exhibits regime change at  $L \approx 24$ : For  $L < 24$ :  $\chi^2(L)/df \approx 1.0 \pm 0.02$  (consistent with uniformity— $\pi$  blocks are effectively random) For  $L > 24$ :  $\chi^2(L)/df > 1.0$  systematically (deviation from uniformity due to collision-induced structure)

Specifically, NMSI predicts:

$$\chi^2(20)/df \approx 0.998 \pm 0.01$$

$$\chi^2(22)/df \approx 1.002 \pm 0.01$$

$$\chi^2(24)/df \approx 1.10 \pm 0.05 \text{ (transition point)} \quad \chi^2(26)/df \approx 1.25 \pm 0.08$$

$$\chi^2(28)/df \approx 1.45 \pm 0.12$$

$$\chi^2(30)/df \approx 1.70 \pm 0.15$$

**Testability:** This prediction is immediately testable using publicly available  $\pi$  digit databases. Y-cruncher and related projects have computed  $\pi$  to over  $10^{14}$  digits, far exceeding the  $10^{12}$  needed for statistically powerful tests. The computational requirements are modest—analysis of  $10^{12}$  digits for blocks up to  $L = 30$  requires approximately  $10^{15}$  operations, achievable in hours on modern hardware.

**Statistical Power Analysis:** For  $M = 10^{10}$  non-overlapping blocks of length  $L = 24$  (requiring  $2.4 \times 10^{11}$   $\pi$  digits), the statistical power to detect  $\chi^2(L)/df = 1.10$  at significance  $\alpha = 0.001$  is  $> 0.999$ . Even conservative effect sizes ( $\chi^2/df = 1.05$ ) are detectable with power  $> 0.95$ .

## Theoretical Architecture: The DZO-OPF-RON Framework

### The Indexing Problem: From $\pi$ -Flow to Physical Constraint

In NMSI, the mathematical constant  $\pi$  serves as an informational seed for a deterministic addressing mechanism that converts abstract mathematical structure into physical constraint. Each block of  $L$  digits from the decimal expansion of  $\pi$  acts as a unique index pointing to nodes within the Riemann Oscillatory Network (RON)—the fundamental substrate of physical reality. This section develops the complete theoretical architecture showing how coherent physics emerges necessarily from this indexing structure [3-30].

**The Core Indexing Hypothesis:** Physical events at spacetime location  $(x, t)$  are determined by RON configuration accessed via  $\pi$ -block addressing. The block index  $k$  is determined by the event's informational coordinate (related to proper time and spatial position through a mapping we do not fully specify here).

The address:

$$A(B_k) = [\sum_{i=0}^{L-1} d(kL+i) \cdot 10^{(L-1-i)}] \bmod N$$

selects which RON nodes are activated, determining local field values, particle interactions, and measurement outcomes.

**The Fundamental Problem:** For  $L > L^* = 24$ , the number of possible blocks ( $10^L$ ) vastly exceeds RON capacity ( $N = 10^{12}$ ), creating inevitable collisions. When distinct blocks  $B_j$  and  $B_k$  map to the same RON address, the system faces an informational ambiguity—multiple inputs demand the same output channel. This is not a bug but a feature: collisions force the system to develop coherence mechanisms for disambiguation. Without such mechanisms, the system would either halt (computational deadlock) or produce inconsistent outputs (physical chaos).

The Causal Chain from  $\pi$  to Physics:

$\pi$  (raw informational flux, infinite, apparently random)

↓

INDEXING ( $L$ -digit block extraction, deterministic)

↓

ADDRESS COMPUTATION (modular arithmetic mod  $N$ )

↓

RON ( $N \approx 10^{12}$  oscillatory nodes, finite capacity)

↓

COLLISION DETECTION ( $L > 24 \Rightarrow$  collisions inevitable)

↓

COHERENCE NECESSITY (system must resolve collisions)

↓

OPF ACTIVATION (geometric mode selection)

↓

DZO ACTIVATION (dynamic balance regulation)

↓

FIXED POINT EMERGENCE (stable physical configuration)

↓

OBSERVABLE PHYSICS (particles, fields, structures)

**The Architectural Threshold:** Why  $L^* = 24$  is Inevitable

The threshold  $L^* = 24$  is not chosen for aesthetic reasons, post-hoc fitting to observations, or numerological appeal. It emerges necessarily from the finite architecture of RON combined with the requirement for collision-free deterministic addressing.

### Theorem 3.1 (Architectural Threshold—Full Statement):

Let RON be a finite oscillatory network with  $N$  nodes, and let  $\pi$ -indexing use  $L$ -digit blocks with modular addressing. Define the collision probability  $P_c(L, M)$  as the probability of at least one address collision among  $M$  consecutive blocks. Then:

(1) For  $L < 2 \cdot \log_{10}(N)$ ,  $P_c \rightarrow 1$  as  $M \rightarrow \infty$  (collisions certain). (2) For  $L > 2 \cdot \log_{10}(N)$ ,  $P_c \rightarrow 0$  as  $M \rightarrow \infty$  at fixed address density  $M/10^L$  (collisions negligible). (3) The transition occurs at  $L^* = 2 \cdot \log_{10}(N) = 24$  for  $N = 10^{12}$ , with transition width  $\Delta L \approx 2$ .

**Complete Proof:** Part (1)—Lower bound on collisions for  $L < 2 \cdot \log_{10}(N)$ : For  $L$ -digit blocks, the address space has size  $10^L$ . Consider  $M$  blocks processed sequentially. By birthday paradox generalization, the expected number of collisions is:

$$E[C] = M(M-1)/(2 \cdot 10^L)$$

For  $M = N = 10^{12}$  and  $L = 22 (< 24)$ , we have  $E[C] = 10^{24}/(2 \cdot 10^{22}) = 50$ . Since  $E[C] \gg 1$ , collisions occur with overwhelming probability. More precisely,  $P_c = 1 - \exp(-M^2/(2 \cdot 10^L)) \rightarrow 1 - \exp(-50) \approx 1$ .

Part (2)—Upper bound on collisions for  $L > 2 \cdot \log_{10}(N)$ : For  $L = 26 (> 24)$  and  $M = 10^{12}$ ,  $E[C] = 10^{24}/(2 \cdot 10^{26}) = 0.005$ . By Markov inequality,  $P_c \leq E[C] = 0.005$ . The system operates essentially collision-free.

Part (3)—Transition sharpness:

The transition function  $P_c(L) = 1 - \exp(-10^{24}/(2 \cdot 10^L))$  has derivative:

$$dP_c/dL = \ln(10) \cdot 10^{(24-L)} \cdot \exp(-10^{(24-L)}/2)/2$$

This is maximal at  $L = 24 - \log_{10}(2) \approx 23.7$ , with width (defined as region where  $0.1 < P_c < 0.9$ ) spanning  $L$  from 23 to 25. The transition is sharp. QED.

**Physical Interpretation:** Below  $L^* = 24$ , the  $\pi$ -indexing system experiences chronic collisions—multiple informational inputs constantly compete for limited RON channels. This corresponds to the 'quantum regime' where uncertainty, superposition, and interference dominate. Above  $L^* = 24$ , addressing becomes effectively collision-free—each input receives dedicated channel. This corresponds to the 'classical regime' where deterministic, non-interfering dynamics prevail.

**The Transition at  $L^* = 24$ :** The regime change at  $L^* = 24$  corresponds to fundamental physics transitions:

- Quantum to classical boundary
- CMB multipole  $\ell \approx 24$  marks anomaly regime boundary
- BAO scale where  $r_d$  uncertainty transitions
- Tornado vortex coherence threshold  $J(rc) = L^* \cdot \ln(10) = 55.26$  nats

### Irreducibility of the DZO-OPF-RON Triad

Given the collision problem for  $L > 24$ , the system requires mechanisms for coherent resolution. We now prove that the DZO-OPF-RON architecture is the minimal structure capable of producing stable, non-trivial physical states from infinite informational input.

**Proposition 3.1 (Irreducibility of the Triad):** Any regime of coherent finite information processing from infinite source requires simultaneously: (i) RON—a finite register of oscillator nodes providing fundamental memory; (ii) OPF—a static selection operator implementing geometric mode filtering; (iii) DZO—a dynamic regulation operator maintaining balance. Elimination of any component leads to exactly one of two outcomes: persistent chaos (entropy divergence) OR trivial collapse (zero information content).

**Proof by Exhaustive Case Analysis:** We consider all possible subsets of the triad and demonstrate failure in each incomplete case.

#### Case 1: No RON (OPF + DZO only, no finite substrate)

Without a finite register to store state, the system has no memory. Each processing cycle is independent of previous cycles. OPF can filter but has nothing to filter from. DZO can regulate but has nothing to regulate. The system reduces to identity operation on transient input—no persistent structure forms. Result: NO PHYSICS POSSIBLE, as there is no medium for information storage or accumulation.

#### Case 2: No OPF (RON + DZO only, no mode selection)

All  $10^L$  possible  $\pi$ -blocks compete equally for  $N$  RON addresses with no preferential filtering. For  $L > 24$ , collision rate exceeds  $N$  per processing cycle. Without geometric filtering to select coherent mode combinations, the collision resolution burden grows exponentially. RON saturates with conflicting instructions. DZO attempts to regulate but receives contradictory balance signals from competing modes. Result: COMPUTATIONAL OVERFLOW, persistent chaos, entropy approaches maximum ( $\log_2(N)$  bits per node).

#### Case 3: No DZO (RON + OPF only, no dynamic regulation)

OPF selects coherent modes from incoming  $\pi$ -blocks, writing to RON. However, without feedback regulation, selected states undergo uncompensated drift. Small perturbations (from residual unfiltered modes) accumulate without correction. Lyapunov analysis: Let  $\Psi(t)$  be RON state,  $\delta\Psi$  small perturbation. Without DZO,  $d(\delta\Psi)/dt = J \cdot \delta\Psi$  where  $J$  is Jacobian with positive eigenvalues (no restoring force). Solution  $\delta\Psi(t) = \delta\Psi(0) \cdot \exp(\lambda_{\max} \cdot t)$  grows exponentially. Result: INITIAL COHERENCE DECAYS, return to chaos on timescale  $1/\lambda_{\max}$ .

**Case 4: RON only (no OPF, no DZO):** Finite memory exists but receives unfiltered, unregulated input from  $\pi$ -indexing. Every  $\pi$ -block writes directly to addressed RON location without selection or balance. Information theory: channel capacity is  $N \cdot \log_2(K)$  where  $K$  is state resolution per node. Input rate from  $\pi$  is unlimited. By Shannon's noisy channel theorem, reliable storage requires input rate  $\leq$  capacity. Without filtering (OPF), effective input rate is infinite. Result: RON SATURATES WITH NOISE, information content approaches zero (maximum entropy, no structure).

**Case 5: RON + OPF only (no DZO):** Modes are selected by OPF's geometric filtering, creating initial coherent patterns in RON. However, without dynamic regulation, these patterns evolve under RON's intrinsic dynamics (coupled oscillator equations). For coupled oscillators without damping or external forcing, generic initial conditions lead to ergodic exploration of energy surface (thermalization). Even starting from coherent configuration, the system explores increasingly incoherent regions of phase space. Result: TRANSIENT STRUCTURE followed by equilibration to thermal state (maximum entropy given energy constraint).

**Case 6: RON + DZO only (no OPF):** DZO maintains balance condition  $G[\Psi] = 0$  for RON state  $\Psi$ , without mode selection. The balance condition is satisfied by the trivial state  $\Psi = 0$  (all nodes quiescent). Without OPF to inject structured information, DZO drives the system toward minimum-variance configuration. For any non-trivial initial state, DZO regulation acts as effective damping, reducing deviations from balance. In absence of structured input from OPF, the unique stable fixed point is  $\Psi^* = 0$ . Result: TRIVIAL COLLAPSE to vacuum state, zero information content.

**Conclusion:** Only the complete triad RON + OPF + DZO produces stable, non-trivial, information-rich physical states. RON provides the finite substrate, OPF provides structured input through geometric selection, and DZO provides stability through dynamic regulation. This is the MINIMAL architecture—adding components may enhance performance but removing any



component destroys coherent physics. QED.

### Operational Phase Funnel (OPF): Gabriel Horn Geometry

The Operational Phase Funnel is not a metaphor but a precise geometric structure implementing scale-dependent mode selection. Its geometry resolves the apparent paradox of finite physics emerging from infinite informational input.

**Definition 3.1 (Gabriel Horn—Mathematical):** The Gabriel Horn (Torricelli's trumpet) is the surface of revolution generated by rotating the curve  $y = 1/x$  about the  $x$ -axis for  $x \geq 1$ . Its defining paradox: finite volume but infinite surface area:

Volume:  $V = \pi \cdot \int_1^\infty (1/x)^2 dx = \pi \cdot [-1/x]_1^\infty = \pi$  (FINITE)  
Surface Area:  $S = 2\pi \cdot \int_1^\infty (1/x) \cdot \sqrt{1 + 1/x^4} dx \geq 2\pi \cdot \int_1^\infty (1/x) dx = \infty$  (INFINITE).

**Definition 3.2 (OPF Geometry):** The OPF is a mapping  $F: \mathbb{R}^+ \rightarrow \mathbb{R}^+$  defined on the informational coordinate  $x \in [1, \infty)$  with weight function  $g(x)$  satisfying:

(P1) Monotonic contraction:  $g'(x) < 0$  for all  $x > 1$  (decreasing weight with scale).

(P2) Positivity:  $g(x) > 0$  for all  $x \geq 1$  (non-negative filtering).

(P3) Finite integral:  $\int_1^\infty g(x) dx < \infty$  (bounded total weight).

(P4) Infinite support:  $g(x) > 0$  for all finite  $x$  (no hard cutoff).

The canonical choice  $g(x) = 1/x^2$  yields the Gabriel Horn geometry. More generally,  $g(x) = x^{-\alpha}$  for  $\alpha > 1$  satisfies P1–P4.

**Lemma 3.1 (Informational Funnel—Gabriel Horn):** Let  $I(x)$  be an informational flux subjected to OPF filtering with weight  $g(x)$  satisfying P1–P4. Define the filtered output:  $I_{\text{filtered}} = \int_1^\infty g(x) \cdot I(x) dx$ . Then:

(1) Finite output: Even for unbounded input ( $I(x) \rightarrow \infty$  as  $x \rightarrow 1$  or  $\infty$ ),  $I_{\text{filtered}} < \infty$ . (2) Scale selection: Modes at scale  $x$  contribute proportionally to  $g(x)$ , strongly suppressing  $x \gg 1$ . (3) Coherence transition: There exists  $x_c < \infty$  such that for  $x > x_c$ , the accumulated filtering constraint exceeds threshold.

### Proof

**Part (1):** For  $I(x)$  bounded by polynomial  $I(x) \leq C \cdot x^\beta$ , the filtered output is:

$$I_{\text{filtered}} \leq C \cdot \int_1^\infty x^{-\alpha} \cdot x^\beta dx = C \cdot \int_1^\infty x^{\beta-\alpha} dx$$

This converges for  $\beta - \alpha < -1$ , i.e.,  $\alpha > \beta + 1$ . Since physical inputs have at most polynomial growth, choosing  $\alpha = 2$  handles all reasonable cases.

**Part (2):** Contribution from scale interval  $[x, x + dx]$  is  $g(x) \cdot I(x) \cdot dx = I(x) \cdot dx/x^2$ . High scales (large  $x$ ) are suppressed by factor  $1/x^2$  regardless of input amplitude.

**Part (3):** Define the constraint accumulation function:

$$J(x) = \int_x^\infty |g'(\xi)|/g(\xi) d\xi = \int_x^\infty \alpha/\xi d\xi = \alpha \cdot \ln(\infty/x)$$

This diverges logarithmically as  $x \rightarrow 1$ , but for any finite  $x_c$ ,  $J(x_c) = \alpha \cdot \ln(R/x_c)$  where  $R$  is the effective outer boundary. The transition point  $x_c$  satisfies  $J(x_c) = \text{threshold value}$  determined by architectural constraint  $L^*$ . QED.

**The Critical Numerical Value:** Setting the constraint threshold equal to the architectural limit:

$$J(x_c) = L^* \cdot \ln(10) = 24 \cdot \ln(10) = 24 \times 2.302585... = 55.26 \text{ nats}$$

This is the constraint accumulation required for coherence emergence—the informational 'cost' of transitioning from chaotic to

coherent regime. It is not adjustable; it derives directly from  $L^* = 24$  via the natural logarithm conversion from decimal to natural information units.

**Physical Interpretation:** OPF acts as a geometric low-pass filter in informational frequency space. High-frequency modes (large  $x$ , corresponding to small spatial scales or high energies) are exponentially suppressed by the  $1/x^2$  falloff. The integrated capacity (volume =  $\pi$ ) represents the total information that can pass through the funnel, while the infinite surface area represents the rich boundary structure available for encoding correlations. This resolves the infinity-to-finite mapping: infinite input diversity is compressed to finite output complexity through geometric filtering, with the compression ratio determined by  $g(x)$  profile.

### Dynamic Zero Operator (DZO): The Regulation Mechanism

The OPF provides geometric selection of coherent modes, but selection alone is insufficient for sustained stability. Physical systems require dynamic regulation to maintain selected states over extended time without continuous external forcing. This is the role of the Dynamic Zero Operator (DZO).

**Definition 3.3 (Balance Condition):** Let  $\Psi(x, t)$  be the RON state field representing the collective configuration of  $N$  oscillatory nodes. Define the balance functional:

$$G[\Psi] = \nabla \cdot (g(x) \cdot \nabla \Psi) - \lambda \cdot \Psi$$

where  $g(x)$  is the OPF weight function and  $\lambda$  is a constant determined by boundary conditions. The balance condition  $G[\Psi^*] = 0$  defines the manifold of balanced states.

**Definition 3.4 (Dynamic Zero Operator):** The DZO acts on RON state as:

$$\text{DZO}[\Psi] = \Psi - \eta \cdot G[\Psi]$$

where  $\eta > 0$  is the regulation step size. This implements gradient descent toward the balance manifold  $G[\Psi] = 0$ .

### Properties of DZO

(x) Fixed points:  $\text{DZO}[\Psi^*] = \Psi^*$  if and only if  $G[\Psi^*] = 0$  (balanced states are fixed points).

(xi) Contraction: For appropriate  $\eta$ , DZO is a contraction mapping. Let  $\Psi_1, \Psi_2$  be two states with  $\|\Psi_1 - \Psi_2\| = \delta$ . Then:

$$\|\text{DZO}[\Psi_1] - \text{DZO}[\Psi_2]\| \leq \kappa \cdot \delta \text{ with } \kappa < 1$$

where  $\kappa = |1 - \eta \cdot \lambda_{\min}(L)|$  and  $L$  is the linear operator associated with  $G$ . Contraction requires  $\eta < 2/\lambda_{\max}(L)$ .

(xii) Convergence: By Banach fixed-point theorem, iteration  $\Psi_{n+1} = \text{DZO}[\Psi_n]$  converges exponentially to unique fixed point  $\Psi^*$  satisfying  $G[\Psi^*] = 0$ :

$$\|\Psi_n - \Psi^*\| \leq \kappa^n \cdot \|\Psi_0 - \Psi^*\|$$

**Physical Interpretation:** DZO implements self-regulation without external forcing. Once OPF has selected coherent modes and written them to RON, the DZO continuously adjusts the configuration toward the balance manifold.

This is analogous to homeostatic regulation in biological systems—the system 'seeks' balance rather than requiring external maintenance. The key difference from dissipative systems (which require energy input to maintain structure) is that DZO operates on informational balance, not energetic forcing. The 'energy' for regulation comes from the informational flux through OPF, not

from external reservoir.

**DZO in Physical Terms:** The balance condition  $G[\Psi^*] = 0$  has physical interpretations depending on context:

- In quantum mechanics:  $G = 0$  corresponds to stationary states (energy eigenstates).
- In thermodynamics:  $G = 0$  corresponds to equilibrium (maximum entropy given constraints).
- In fluid dynamics:  $G = 0$  corresponds to steady flow (time-independent velocity field).
- In cosmology:  $G = 0$  corresponds to de Sitter attractor (constant Hubble parameter).

The universality of balance-seeking behavior across physics reflects the universal operation of DZO across RON substrate.

### Fixed-Point Coincidence Theorem

The central result connecting OPF geometric selection and DZO dynamic regulation establishes that their fixed points coincide when properly configured. This theorem guarantees the existence of stable, physically observable states.

**Theorem 3.2 (OPF-DZO Fixed-Point Coincidence):** Let  $F$  be an OPF satisfying properties P1–P4 with weight function  $g(x)$ , and let DZO be defined with balance operator  $G$  derived from  $g$  via  $G[\Psi] = \nabla \cdot (g \cdot \nabla \Psi) - \lambda \cdot \Psi$ . Define the combined operator  $T = \text{OPF} \circ \text{DZO}$ . Then: (1) Existence:  $\text{Fix}(\text{OPF}) \cap \text{Fix}(\text{DZO}) \neq \emptyset$ . (2) Uniqueness: The intersection contains exactly one element:  $\text{Fix}(\text{OPF}) \cap \text{Fix}(\text{DZO}) = \{\Psi^*\}$ . (3) Stability:  $\Psi^*$  is asymptotically stable under iteration of  $T$ : for any  $\Psi_0$ ,  $T^n(\Psi_0) \rightarrow \Psi^*$  as  $n \rightarrow \infty$ . (4) Physical Observability:  $\Psi^*$  corresponds to coherent physical states (particles, fields, structures).

### Proof

**Part (1)—Existence:** The OPF defines a coherence functional:

$$\text{FOPF}[\Psi] = \int_{\mathbb{R}^d} g(x) \cdot |\nabla \Psi|^2 dx$$

OPF selects states minimizing FOPF subject to normalization constraint  $\int |\Psi|^2 = 1$ . By calculus of variations, minimizers satisfy Euler-Lagrange equation:

$$\delta \text{FOPF} / \delta \Psi = -2 \cdot \nabla \cdot (g \cdot \nabla \Psi) + 2\lambda \Psi = 0$$

where  $\lambda$  is Lagrange multiplier. This is exactly  $G[\Psi] = 0$  (up to factor  $-2$ ). Therefore,  $\text{Fix}(\text{OPF}) \subseteq \{\Psi : G[\Psi] = 0\} = \text{Fix}(\text{DZO})$ . Since FOPF is strictly convex and coercive on  $H^1$  function space, a minimizer exists. Therefore  $\text{Fix}(\text{OPF}) \cap \text{Fix}(\text{DZO}) \neq \emptyset$ .

**Part (2)—Uniqueness:** Suppose  $\Psi_1$  and  $\Psi_2$  are both in  $\text{Fix}(\text{OPF}) \cap \text{Fix}(\text{DZO})$ . Then both minimize FOPF. By strict convexity of FOPF (coming from the  $|\nabla \Psi|^2$  term), the minimizer is unique (up to global phase). Therefore  $\Psi_1 = \exp(i\phi) \cdot \Psi_2$  for some phase  $\phi$ . Since physical states are phase-equivalence classes,  $\Psi^*$  is unique.

**Part (3)—Stability:** The combined operator  $T = \text{OPF} \circ \text{DZO}$  satisfies:  $T[\Psi^*] = \text{OPF}[\text{DZO}[\Psi^*]] = \text{OPF}[\Psi^*] = \Psi^*$  (since  $\Psi^* \in \text{Fix}(\text{DZO})$  and  $\text{Fix}(\text{OPF})$ ). For  $\Psi$  near  $\Psi^*$ , linearize:  $T[\Psi^* + \delta] \approx T[\Psi^*] + DT[\Psi^* \cdot \delta] = \Psi^* + DT \cdot \delta$ . The linearization  $DT$  is product of linearized OPF (projection onto low-FOPF subspace) and linearized DZO (contraction toward  $G = 0$  manifold). Both have

spectral radius  $< 1$  for transverse directions, so  $DT$  has spectral radius  $< 1$ . By spectral theory,  $T^n \cdot \delta \rightarrow 0$ , proving asymptotic stability.

**Part (4)—Physical Observability:** States  $\Psi^*$  minimizing FOPF subject to normalization have minimal 'informational complexity' consistent with non-triviality. This corresponds to stable, distinguishable configurations—precisely what we call

**'Physical Significance':** Theorem 3.2 guarantees that the NMSI architecture produces exactly one type of stable output: coherent physical states satisfying both geometric selection (OPF) and dynamic balance (DZO). This explains why physics has definite, reproducible character—the universe converges to unique fixed points rather than wandering chaotically or collapsing trivially. The coincidence  $\text{Fix}(\text{OPF}) = \text{Fix}(\text{DZO}) = \{\Psi^*\}$  is not imposed but derived from the mathematical structure relating OPF weight  $g(x)$  and DZO balance operator  $G$ .

### Why $\pi$ Appears 'Chaotic' Before $L^* = 24$ and Correlates with Riemann Zeta After

The statistical behavior of  $\pi$ -digit blocks exhibits a sharp transition at  $L = 24$ , directly reflecting the RON architectural constraint. This provides the key testable signature of NMSI.

For  $L < 24$  (Pre-threshold Regime):

- Address space ( $10^L$ )  $\ll$  RON capacity ( $10^{12}$ )
- Collisions are rare (expected number  $\ll 1$  for typical  $M$ )
- Each  $\pi$ -block maps to effectively unique RON node
- No correlation structure is forced by finite RON
- Result:  $\pi$ -blocks behave as independent random samples
- Statistical signature: pass all standard randomness tests (NIST SP 800-22)
- $\chi^2(L)/df \approx 1.0$

For  $L > 24$  (Post-threshold Regime):

- Address space ( $10^L$ ) vastly exceeds RON capacity ( $10^{12}$ )
- Collisions are frequent (expected number  $\gg 1$ )
- Multiple  $\pi$ -blocks map to same RON node
- Collision resolution forces correlations between blocks sharing nodes
- Result:  $\pi$ -blocks exhibit structured dependencies reflecting RON topology
- Statistical signature: fail randomness tests for subtle correlations
- $\chi^2(L)/df > 1.0$  systematically

**The  $\pi$ -Riemann Zeta Connection:** RON is defined by  $\zeta$ -zeros. When collisions force  $\pi$ -blocks to share RON nodes, the block statistics inherit properties of the  $\zeta$ -zero distribution. Specifically:

1. The  $\zeta$ -zeros exhibit GUE (Gaussian Unitary Ensemble) pair correlation:

$$R_2(\alpha) = 1 - (\sin(\pi\alpha)/(\pi\alpha))^2$$

where  $\alpha$  is the normalized zero spacing.

2. For  $L > 24$ , collision-linked  $\pi$ -blocks share RON nodes at positions  $\{n_1, n_2, \dots\}$  determined by  $\zeta$ -zeros.
3. The spacing distribution of collision-linked block indices should converge to GUE pair correlation.

### Testable Prediction ( $\pi$ -Riemann Zeta Correlation):

For  $L \in \{20, 22, 24, 26, 28, 30\}$ , compute collision events (dis-



tinct blocks mapping to same address mod  $N = 10^{12}$ ).

Analyze spacing distribution of collision-linked block indices.  
Expected results:

$L \leq 22$ : Poisson spacing distribution (independent, uncorrelated)

$L = 24$ : Transition region (partial correlations)

$L \geq 26$ : GUE spacing distribution ( $\zeta$ -like correlations)

This prediction is immediately testable using available  $\pi$ -digit databases ( $10^{13}+$  digits computed) and requires only standard statistical analysis.

### Physical Implementations

#### General Principle: From $\pi$ -Indexing to Observable Structures

The abstract DZO-OPF-RON architecture maps to physical observables through a consistent causal chain. Every stable physical structure emerges as a manifestation of an OPF-DZO fixed point in RON phase space. The architectural threshold  $L^* = 24$  appears universally wherever coherent structure emerges from underlying informational chaos.

**The Universal Implementation Principle:** For any physical system exhibiting coherent structure (atoms, CMB acoustic peaks, tornado cores, galaxy clusters), there exists a mapping from system parameters to RON addressing such that:

1. The system's characteristic scale corresponds to block length  $L$  in the  $\pi$ -indexing.
2. Coherence emerges at  $L = L^* = 24$  (or corresponding physical scale).
3. The coherent configuration is the unique fixed point  $\Psi^*$  from Theorem 3.2.
4. Observable properties derive from  $\Psi^*$  via appropriate projection operators.

**Scale Correspondence:** The block length  $L$  maps to physical scales via:

$$\text{Scale}(L) = \ell \text{Planck} \cdot 10^{(L/2)}$$

where  $\ell \text{Planck} = 1.6 \times 10^{-35}$  m. For  $L = 24$ :

$$\text{Scale}(24) = 1.6 \times 10^{-35} \cdot 10^{12} \text{ m} = 1.6 \times 10^{-23} \text{ m} \approx 10 \text{ fm}$$

This is the nuclear scale, where quantum coherence transitions to classical behavior. The correspondence extends to angular scales in CMB ( $\ell \approx L$ ), frequency scales in BAO, and radial scales in vortex dynamics.

#### CMB Low- $\ell$ Anomalies as OPF Transition Signatures

The Cosmic Microwave Background exhibits well-documented anomalies at large angular scales (multipoles  $\ell < 30$ ) that have persisted across COBE, WMAP, and Planck observations. NMSI interprets these as signatures of the OPF transition at  $\ell_c \approx 24$ .

**The CMB-RON Correspondence:** CMB multipoles  $\ell$  correspond to RON addressing length  $L$  through the informational mapping:

$$\ell \leftrightarrow L \text{ (angular scale} \leftrightarrow \text{block length)}$$

**The physical basis:** CMB anisotropies at multipole  $\ell$  contain  $(2\ell + 1)$  independent modes (the spherical harmonic coefficients  $a_{\ell m}$  for  $m = -\ell$  to  $+\ell$ ). The total information content at scale  $\ell$  is approximately  $\ell$  bits. This maps directly to  $L$ -digit blocks containing  $L \cdot \log_2(10) \approx 3.3 \cdot L$  bits.

**Low- $\ell$  (large angular scales) corresponds to short blocks ( $L$**

**< 24):**

- Few RON nodes addressed per sky patch
- Minimal collision-induced correlations
- Independent, uncorrelated mode behavior
- High entropy (maximum uncertainty given constraints)

**High- $\ell$  (small angular scales) corresponds to long blocks ( $L > 24$ ):**

- Many RON nodes addressed, collisions common
- Collision-induced correlations structure the modes
- Coherent, correlated mode behavior
- Lower entropy (structure reduces uncertainty)

#### NMSI Explanation of Specific CMB Anomalies:

**a. Quadrupole Suppression ( $\ell = 2$ ):** At  $\ell = 2$ , the system is deep in pre-threshold regime with  $L \ll 24$ . Only  $10^2 = 100$  effective addresses exist, far below RON capacity of  $10^{12}$ . The OPF has minimal filtering effect—modes pass nearly unselected, without the coherence enhancement that occurs for  $\ell > 24$ . Result: power suppression relative to  $\Lambda$ CDM predictions that assume scale-invariant initial conditions. The observed quadrupole power is approximately 70% of predicted, consistent with pre-OPF unenhanced transmission.

**b. Quadrupole-Octopole Alignment:** For  $\ell \in \{2, 3\}$ , addressing is unconstrained—blocks can map anywhere in RON without collision pressure. Without collision-induced correlations forcing specific configurations, modes align along whatever symmetry axes exist in RON's intrinsic structure (related to  $\zeta$ -zero distribution). Result: the quadrupole and octopole planes align with ecliptic plane (probability  $< 0.1\%$  under  $\Lambda$ CDM isotropy assumption) reflecting RON's preferred directions.

**c. Hemispherical Power Asymmetry:** The OPF transition at  $\ell_c \approx 24$  creates a boundary between uncorrelated ( $\ell < 24$ ) and correlated ( $\ell > 24$ ) regimes. Modes near this boundary experience partial filtering—some directions receive more OPF coherence enhancement than others depending on geometric projection onto RON structure. Result: north-south asymmetry of approximately 6% in variance, with transition occurring around  $\ell \approx 20$ –30.

**d. The Cold Spot:** The large under-density at Galactic coordinates  $(l, b) = (209^\circ, -57^\circ)$  with angular size  $\approx 5^\circ$  corresponds to multipole  $\ell \approx 36$  (just above threshold). At this scale, OPF is fully active, creating coherent under-densities where RON collision patterns destructively interfere. The Cold Spot represents a 'coherent void'—an OPF-DZO fixed point with negative temperature fluctuation. Its apparent 'significance' ( $< 1\%$  probability) reflects that coherent structures are rare—most fixed points have smaller amplitude.

**Testable Prediction—CMB Spectral Entropy:** Define the spectral entropy at multipole  $\ell$ :

$$H(\ell) = -\sum_{m=-\ell}^{\ell} \left( \frac{|a_{\ell m}|^2}{C_\ell} \right) \cdot \log \left( \frac{|a_{\ell m}|^2}{C_\ell} \right)$$

where  $C_\ell = (1/(2\ell+1)) \cdot \sum |a_{\ell m}|^2$  is the angular power spectrum. For isotropic Gaussian field,  $H(\ell) = \log(2\ell+1)$  (maximum entropy).

#### NMSI Prediction:

For  $\ell < 24$ :  $H(\ell) \approx \log(2\ell+1)$  (uncorrelated, maximum entropy)  
For  $\ell > 24$ :  $H(\ell) < \log(2\ell+1)$  (correlated, reduced entropy)  
Transition at  $\ell_c = 24 \pm 5$  The ratio  $H(\ell)/\log(2\ell+1)$  should drop

from  $\approx 1.0$  for  $\ell < 20$  to  $\approx 0.85\text{--}0.90$  for  $\ell > 30$ , with transition around  $\ell = 24$ .

### BAO Drift as DZO Cyclic Regulation

Baryon Acoustic Oscillations provide a 'standard ruler' at comoving scale  $rd \approx 147$  Mpc, supposedly fixed at recombination ( $z \approx 1100$ ).  $\Lambda$ CDM treats  $rd$  as a frozen scale determined by pre-recombination physics, unchanging thereafter. Recent observations suggest subtle deviations from this frozen ruler paradigm.

**NMSI Interpretation:** The BAO scale is not frozen but undergoes DZO-regulated oscillations tied to the cosmic cycle parameter  $Z$ . The Dynamic Zero Operator maintains global informational balance, but balance is defined relative to cycle phase. As  $Z$  evolves from  $-20$  (previous turnaround) through  $Z_{\text{now}} = +12$  toward  $Z = +20$  (next turnaround), the DZO set-point shifts, causing periodic adjustment of large-scale structure parameters including  $rd$ .

**Mathematical Model:** Define the effective BAO scale as function of cycle parameter:

$$rd(Z) = rd^{(0)} \cdot [1 + \varepsilon \cdot \sin(\pi Z/20)]$$

where  $rd^{(0)} = 147$  Mpc is the mean scale and  $\varepsilon \approx 0.01$  is the DZO regulation amplitude. The sinusoidal form reflects the cyclic nature with  $Z \in [-20, +20]$ .

### Observable Consequences:

#### 1. For current epoch $Z_{\text{now}} = +12$ :

$\Delta rd/rd = \varepsilon \cdot \sin(12\pi/20) = 0.01 \cdot \sin(0.6\pi) = 0.01 \cdot 0.951 = 0.95\%$   
This approximately 1% deviation is consistent with the 2–3 $\sigma$  tensions reported between DESI BAO measurements and Planck-derived  $\Lambda$ CDM parameters.

**2. Redshift dependence:** Different redshifts probe different cosmic epochs with different  $Z$  values. The  $Z$ -to-redshift mapping (non-trivial in cyclic cosmology) gives:

$z = 0.5$  ( $Z \approx 14$ ):  $\Delta rd/rd = \varepsilon \cdot \sin(14\pi/20) = +0.59\%$   $z = 1.0$  ( $Z \approx 10$ ):  $\Delta rd/rd = \varepsilon \cdot \sin(10\pi/20) = +1.00\%$   $z = 2.0$  ( $Z \approx 6$ ):  $\Delta rd/rd = \varepsilon \cdot \sin(6\pi/20) = +0.81\%$ .

**3. Pattern:** The drift follows sinusoidal  $Z$ -cycle, not monotonic evolution. This distinguishes NMSI from dark energy models (monotonic deviation) and modified gravity (scale-dependent deviation).

**Falsification Criteria:** If DESI/Euclid measurements through 2028 show BAO scale evolution inconsistent with sinusoidal  $Z$ -cycle pattern (e.g., monotonic drift with redshift, or no drift detectable at 1% precision), the DZO regulation model is falsified.

### Early JWST Galaxies as Previous-Cycle Structures

JWST has revealed unexpectedly massive, mature, and chemically evolved galaxies at redshifts  $z > 10$ , posing the 'impossibly early galaxy problem' for  $\Lambda$ CDM. NMSI resolves this through cyclic cosmology: these galaxies are not 'impossibly young' but inherited from the previous cosmic cycle.

**Cyclic Cosmology Framework:** The universe oscillates be-

tween  $Z = -20$  (minimum extension / maximum compression at turnaround) and  $Z = +20$  (maximum extension / minimum compression at next turnaround). Key parameters:

Cycle duration:  $T_{\text{cycle}} \approx 2 \times 10^{11}$  years

Current cycle position:  $Z_{\text{now}} = +12$  (late expansion phase)  
Apparent 'age' in  $\Lambda$ CDM: 13.8 Gyr (time since  $Z = -20$  turnaround)  
Actual elapsed time since previous maximum:  $\approx 6 \times 10^{10}$  years.

**Number of completed cycles:** infinite (eternal cyclic) Baryon Recycling Mechanism: At cyclic turnaround ( $Z = \pm 20$ ), the universe reaches maximum compression but does NOT collapse to singularity. The DZO regulation prevents infinite compression through informational coherence constraints—the fixed-point  $\Psi^*$  has non-zero extent. During turnaround:

1. Most diffuse matter-energy undergoes quantum vacuum restructuring (effective 'reset').
2. Compact structures (stellar cores, neutron star material, black holes) partially survive due to high coherence / low DZO deviation.
3. Heavy elements synthesized in previous cycle remain in surviving compact structures.
4. Large-scale gravitational potential wells partially persist as 'structural seeds'.
5. New expansion begins seeded with recycled baryons and surviving structure.

### Explanation of Specific JWST Observations:

**a. High Stellar Masses at  $z > 10$ :** Galaxies like JADES-GS-z13-0 with stellar mass  $> 10^9 M_{\odot}$  at  $z = 13.2$  contain stellar material that formed primarily in the previous cycle ( $Z$  around  $-10$  to  $0$ ), accumulated through approximately  $10^{11}$  years of star formation, survived turnaround in compact form, and reactivated in current cycle appearing 'already formed'. The apparent mass is not anomalous given  $10^{11}$  year formation timescale (versus 400 Myr in  $\Lambda$ CDM interpretation).

**b. High Metallicity at  $z > 10$ :** Super-solar metallicities observed in some  $z > 10$  galaxies (Curti et al. 2023) reflect cumulative stellar processing over multiple generation cycles, not rapid local enrichment. Elements heavier than iron require neutron star mergers and supernovae over Gyr timescales—impossible in 400 Myr but natural over  $10^{11}$  year cycle.

**c. Disk and Bulge Morphology:** Rotationally supported disk structures require approximately 10 dynamical times to establish ( $t_{\text{dyn}} \approx 10^8$  yr at  $z = 10$ , requiring  $\approx 1$  Gyr). JWST observations of disk galaxies at  $z > 10$  are consistent with previous-cycle dynamical evolution followed by structure preservation through turnaround.

**d. Quiescent Populations:** Some  $z > 10$  galaxies appear 'quenched' with evolved stellar populations and little ongoing star formation. In  $\Lambda$ CDM this is paradoxical (how can a 400 Myr old galaxy be already quenched?). In NMSI, these represent galaxies whose star formation completed in previous cycle and which have not yet restarted in current cycle.

### Testable Predictions:

1. Stellar Age Bimodality: At  $z > 10$ , spectroscopic stellar population analysis should reveal bimodal age distribution—'young' stars ( $< 0.5$  Gyr, formed in current cycle) and

'old' stars (ages inferred  $> 1$  Gyr, inherited from previous cycle). Single-age stellar population models should provide poor fits.

2. Chemical Anomalies: Abundance patterns in some  $z > 10$  galaxies should show inconsistencies with standard stellar yield predictions—specifically, r-process enhancement (from previous-cycle neutron star mergers) and possible isotopic anomalies.
3. Galaxy Number Excess: The cumulative galaxy count at  $z > 12$  should exceed  $\Lambda$ CDM predictions by factor  $> 3$  at  $5\sigma$  confidence (JWST data through 2027).
4. Kinematic Signatures: High- $z$  galaxies with previous-cycle components should show complex kinematics (multiple stellar components with different velocity dispersions) inconsistent with single-formation-episode models.

## NMSI Part 2

### The $\pi$ -Indexed Riemann Oscillatory Network Falsification Principles

NMSI is constructed as a falsifiable scientific framework in the Popperian sense. Unlike speculative cosmologies that accommodate any observation through post-hoc parameter adjustment, NMSI makes specific numerical predictions derived from first principles with explicit thresholds that cannot be retroactively modified. The architectural threshold  $L^* = 24$  and the coherence value  $x_c = 55.26$  nats are mathematical necessities, not adjustable parameters.

able parameters.

**Core Falsification Criteria:** NMSI makes specific commitments that, if violated, definitively refute the framework:

**(F1) CMB Spectral Entropy:** If  $H(\ell)/\log(2\ell+1)$  shows NO transition near  $\ell_c = 24 \pm 5$ , the OPF transition model is falsified.

**(F2)  $\pi$ -Block  $\chi^2$  Statistics:** If  $\chi^2(L)/df$  shows NO transition at  $L = 24 \pm 2$ , the architectural threshold derivation is falsified.

**(F3)  $\pi$ - $\zeta$  GUE Correlation:** If collision-linked block spacings show Poisson (not GUE) statistics for

$L \geq 26$ , the RON connection to  $\zeta$ -zeros is falsified.

**(F4) Tornado Constraint Integral:** If  $J(rc)$  consistently falls outside  $[45, 65]$  nats across 20+ tornado cases, the OPF geometric prediction is falsified.

**(F5) BAO Scale Evolution:** If BAO scale shows NO cyclic drift pattern detectable at 1% precision by 2030, the DZO regulation model is falsified.

**(F6) Galaxy Counts at  $z > 12$ :** If galaxy number density is CONSISTENT with  $\Lambda$ CDM predictions (within  $2\sigma$ ), NMSI loses primary cyclic cosmology support.

These criteria are hierarchically organized: (F1)–(F4) test the mathematical core ( $L^* = 24$ ,  $x_c = 55.26$ ), while (F5)–(F6) test cosmological applications. Failure in the first group falsifies NMSI entirely; failure in the second group constrains its scope.

### Complete Predictions Table

**Table 1:** The following table summarizes twelve falsifiable predictions with instruments, timelines, specific thresholds, and confidence levels required for validation or falsification:

#	Prediction	Observable	NMSI Threshold	Instrument	Timeline
1	CMB entropy transition	$H(\ell)/H_{\max}$ ratio	$\ell_c = 24 \pm 5$	Planck 2018	2025
2	BAO cyclic drift	$rd(z)$ variation	$\Delta rd/rd \approx 1\%$	DESI/Euclid	2025–2028
3	Galaxy excess $z > 12$	$N_{gal}/N_{\Lambda CDM}$	$> 3\times$ at $5\sigma$	JWST	2025–2027
4	Stellar age bimodality	Age distribution	2 peaks at $> 3\sigma$	JWST NIRSpec	2026–2028
5	$\pi$ -block $\chi^2$ jump	$\chi^2(L)/df$	Jump at $L=24\pm 2$	Computation	2025
6	$\pi$ - $\zeta$ GUE correlation	Spacing statistics	GUE for $L \geq 26$	Computation	2025
7	Tornado $J(rc)$	Constraint integral	$55.26 \pm 10$ nats	DOW/VORTEX	2025–2027
8	$H_0$ $z$ -dependence	$H_0(z)$ evolution	$\Delta \approx 3\text{--}5$ km/s/Mpc	SH0ES+DESI	2026–2028
9	GW cycle signature	Stochastic background	Modulation $> 2\sigma$	LISA	2034–2035
10	CMB-BAO consistency	Joint $\chi^2$ fit	$\chi^2_{NMSI} < \chi^2_{\Lambda CDM}$	Combined	2027–2029
11	Chemical anomalies	$[X/Fe]$ patterns	Non-standard at $z > 10$	JWST NIRSpec	2026–2030
12	Primordial GW absence	Tensor ratio $r$	$r < 0.001$	CMB- S4/Lite-BIRD	2030–2035

### Immediately Executable Tests (2025)

Three predictions can be tested immediately using publicly available data and standard computational resources. These provide rapid initial validation or falsification of NMSI core claims without requiring new observations or expensive experiments.

#### TEST #1: CMB Spectral Entropy Transition

**Data Source:** Planck 2018 SMICA component-separated temperature map, available from Planck Legacy Archive (<https://pla.esac.esa.int/>). File: COM\_CMB\_IQU-smica\_2048\_R3.00\_full.fits.

#### Computational Procedure:

**Step 1:** Load Planck SMICA temperature map at HEALPix res-



olution  $N_{\text{side}} = 2048$ .

**Step 2:** Apply UT78 galactic mask to remove foreground-contaminated regions (approximately 22% sky masked).

**Step 3:** Compute spherical harmonic coefficients  $a_{\ell m}$  using HEALPix anafast function for  $\ell = 2$  to 100.

**Step 4:** For each multipole  $\ell$ , compute angular power spectrum  $C_\ell = (1/(2\ell+1)) \times \sum_m |a_{\ell m}|^2$ .

**Step 5:** Compute normalized mode amplitudes  $p_{\ell m} = |a_{\ell m}|^2 / ((2\ell+1) \times C_\ell)$ .

**Step 6:** Compute spectral entropy  $H(\ell) = -\sum_m p_{\ell m} \times \log(p_{\ell m})$ .

**Step 7:** Compute maximum entropy  $H_{\text{max}}(\ell) = \log(2\ell+1)$ .

**Step 8:** Compute normalized ratio  $R(\ell) = H(\ell) / H_{\text{max}}(\ell)$ .

**Step 9:** Plot  $R(\ell)$  versus  $\ell$  for  $\ell = 2$  to 100.

**Step 10:** Identify transition point  $\ell_c$  where  $R(\ell)$  exhibits significant decrease ( $> 5\%$  drop).

**NMSI Prediction:** Sharp transition at  $\ell_c = 24 \pm 5$ . Specifically:  $R(\ell) \approx 0.95\text{--}1.00$  for  $\ell < 20$  (uncorrelated, maximum entropy regime)  $R(\ell) \approx 0.85\text{--}0.92$  for  $\ell > 30$  (correlated, reduced entropy regime) Transition occurs in range  $\ell = 20\text{--}28$ .

**Falsification Criterion:** If  $R(\ell)$  remains flat ( $\pm 0.03$ ) across  $\ell = 15$  to 40 with no detectable transition, the OPF model is falsified at  $> 3\sigma$  confidence.

**Computational Requirements:** Standard laptop with Python, healpy, numpy. Runtime approximately 10 minutes.

**TEST #5:  $\pi$ -Block  $\chi^2$  Transition**

**Data Source:** Pre-computed  $\pi$  digits from y-cruncher project ( $10^{13}+$  digits available). Download from: <http://www.numberworld.org/y-cruncher/> Computational Procedure:

**Step 1:** Load  $\pi$  digits file (minimum  $10^{11}$  digits required for statistical power).

**Step 2:** For each  $L \in \{18, 20, 22, 24, 26, 28, 30\}$ :

**Step 2a:** Extract non-overlapping  $L$ -digit blocks  $B_k$  for  $k = 0$  to  $[N_{\text{digits}}/L] - 1$ .

**Step 2b:** Compute address  $A_k = \text{int}(B_k) \bmod N$  where  $N = 10^{12}$ .

**Step 2c:** Count frequency  $O_a$  of each address  $a \in [0, N-1]$ .

**Step 2d:** Compute expected frequency  $E = M/N$  where  $M$  = number of blocks.

**Step 2e:** Compute  $\chi^2 = \sum_a (O_a - E)^2/E$  summing over addresses with  $O_a > 0$ .

**Step 2f:** Compute degrees of freedom  $df$  = number of unique addresses  $- 1$ .

**Step 2g:** Record  $\chi^2/df$ .

**Step 3:** Plot  $\chi^2(L)/df$  versus  $L$ .

**Step 4:** Identify regime change at  $L \approx 24$ .

**NMSI Prediction:** Regime change at  $L^* = 24 \pm 2$ :

$\chi^2(L)/df \approx 1.00 \pm 0.02$  for  $L \leq 22$  (uniform distribution, no structure)  $\chi^2(L)/df \approx 1.05\text{--}1.15$  for  $L = 24$  (transition point)

$\chi^2(L)/df \approx 1.20\text{--}1.50$  for  $L \geq 26$  (collision-induced correlations)

$\chi^2(L)/df$  increasing approximately as  $(L - 24)^2$  for  $L > 24$

**Falsification Criterion:** If  $\chi^2(L)/df$  remains within  $[0.98, 1.02]$  for ALL  $L$  from 20 to 30, the architectural threshold model is falsified.

**Computational Requirements:** Workstation with 32+ GB RAM. Runtime approximately 2–4 hours for full analysis.

**TEST #6:  $\pi$ - $\zeta$  GUE Correlation.**

**Data Source:** Same  $\pi$  digits as Test #5, plus Odlyzko's tabulated Riemann zeta zeros (first  $10^{12}$  zeros available).

## Computational Procedure

**Step 1:** For  $L = 26$  (above threshold), identify all collision events: pairs  $(B_j, B_k)$  with  $j \neq k$  mapping to same address  $A_j = A_k$ .

**STEP 2:** For each collision, record the block index difference  $\Delta = |j - k|$ .

**Step 3:** Normalize spacings:  $s_i = \Delta_i / \text{mean}(\Delta)$ .

**Step 4:** Compute pair correlation function  $R_2(s)$  from histogram of normalized spacings. Step 5: Compare  $R_2(s)$  to:

- Poisson prediction:  $R_2^{\text{Poisson}}(s) = 1$  (constant, independent)
  - GUE prediction:  $R_2^{\text{GUE}}(s) = 1 - (\sin(\pi s)/(\pi s))^2$
- Step 6: Compute  $\chi^2$  goodness-of-fit to both models. Step 7: Repeat for  $L = 22$  (below threshold) as control.

**NMSI Prediction:** For  $L \leq 22$ : Poisson spacing ( $\chi^2_{\text{Poisson}} \ll \chi^2_{\text{GUE}}$ ) For  $L \geq 26$ : GUE spacing ( $\chi^2_{\text{GUE}} \ll \chi^2_{\text{Poisson}}$ ) Transition at  $L = 24 \pm 2$ .

**Falsification Criterion:** If  $L = 26, 28, 30$  ALL show Poisson spacing ( $\chi^2_{\text{Poisson}} < \chi^2_{\text{GUE}}$ ), the  $\pi$ - $\zeta$  correlation model is falsified.

**Physical Significance:** This test directly probes whether RON (defined by  $\zeta$ -zeros) influences  $\pi$ -block statistics through collision-induced correlations. GUE statistics would confirm that the  $\zeta$ -zero distribution propagates through RON to observable  $\pi$ -block structure.

## Strategic Falsification Hierarchy

The twelve predictions have different implications for NMSI if falsified. We organize them into three tiers based on their diagnostic power:

### TIER 1 — Core Falsification (single negative result refutes NMSI):

**Test #1 (CMB entropy):** Probes OPF transition at  $\ell_c = 24$ . Negative result falsifies the entire OPF geometric selection model—the core mechanism of coherence emergence.

**Test #5 ( $\pi$ -block  $\chi^2$ ):** Probes architectural threshold  $L^* = 24$ . Negative result falsifies the RON collision derivation and undermines the entire  $L^* = 24$  framework.

**Test #7 (Tornado J(rc)):** Probes universal  $\chi_c = 55.26$  prediction. Negative result falsifies the claim that OPF geometry has physical manifestation across scales. If ANY of Tests #1, #5, #7 yield negative results at  $3\sigma$  confidence, NMSI is definitively falsified. These tests probe the mathematical core, not peripheral applications.

### TIER 2 — Strong Constraint (negative results substantially weaken NMSI):

**Test #2 (BAO drift):** Probes DZO cyclic regulation. Negative result would require abandoning the cosmic cycle model while potentially preserving the mathematical framework.

**Test #3 ( $z > 12$  galaxies):** Probes previous-cycle inheritance. Negative result would require alternative explanation for JWST early galaxies, weakening cyclic cosmology support.

**Test #8 ( $H_0$   $z$ -dependence):** Probes cyclic redshift interpretation. Negative result would require alternative Hubble tension resolution within NMSI, if one exists. Negative results in Tier 2 would not directly falsify NMSI mathematical foundations but would significantly reduce its explanatory scope and attractiveness as a comprehensive cosmological framework.

### TIER 3 — Supporting Evidence (negative results require refinement):

Tests #4, #6, #9–12 provide additional confirmation or constrain secondary parameters. Negative results would require model refinement (adjusting  $\epsilon$ , mapping functions, etc.) but would not falsify the core  $L^* = 24$  architecture.

The hierarchical structure ensures that NMSI makes genuine empirical commitments while distinguishing core principles from derived applications. This avoids the common problem of unfalsifiable theories that can accommodate any observation through auxiliary hypotheses.

### Experimental Validation: Tornado Vortex Dynamics

#### Rationale: Why Tornado as Laboratory

The atmospheric tornado (mesocyclonic vortex) provides a unique terrestrial laboratory for validating the DZO-OPF architecture. This is NOT metaphor or analogy—it is direct experimental validation of informational mechanics operating in classical fluid dynamics. The tornado exhibits spontaneous coherence emergence from turbulent flow, precisely the phenomenon that DZO-OPF-RON describes at cosmic scales.

#### Key Advantages of Tornado Validation:

1. **Accessibility:** Tornado velocity data from DOW (Doppler on Wheels) and VORTEX field campaigns is publicly available through NCAR/EOL data archives. No new observations are required—decades of high-resolution radar data exist.
2. **Repeatability:** Multiple tornado cases (50+ documented EF2+ events in VORTEX-2 alone) provide statistical sample for validation. Individual measurement uncertainties average out over ensemble.
3. **Measurability:** Mobile Doppler radar provides direct velocity field measurements at 30–75 meter resolution, 6–10 second temporal cadence, and full volumetric coverage. The three coherence indicators ( $I_1$ ,  $I_2$ ,  $\Omega$ ) map directly to measurable quantities.
4. **Theoretical Clarity:** Vortex dynamics are well-understood in fluid mechanics, with governing equations (Navier-Stokes) fully characterized. The transition from turbulent to coherent flow is phenomenologically clear, enabling unambiguous comparison with NMSI predictions.
5. **Independence:** Tornado physics operates at completely different scales (100 m vs 100 Mpc), energies ( $10^{12}$  J vs  $10^{60}$  J), and timescales (minutes vs Gyr) from cosmological phenomena. Agreement would demonstrate scale-independent universality of OPF-DZO architecture, not merely consistency within one domain.

**Central Claim:** The transition from turbulent exterior to coherent core in tornado vortices exhibits the SAME mathematical structure as the OPF transition at  $L^* = 24$  in  $\pi$ -indexing. Specifically, the constraint accumulation integral  $J(r)$  evaluated at the coherence transition radius  $r_c$  satisfies:

$$J(r_c) = 55.26 \pm 10 \text{ nats}$$

This value is NOT adjustable—it derives directly from  $L^* \times \ln(10) = 24 \times 2.302585 = 55.26$ . The prediction is parameter-free.

#### Observable Structure: Three-Zone Model

Tornado vortices exhibit characteristic three-zone structure ob-

servable in Doppler radar velocity fields. This structure maps directly onto OPF geometry.

Zone 1 — Exterior ( $r > r_{ext}$ ):

**Characteristics:** Turbulent inflow from ambient environment. Velocity field  $V(r, \theta, z)$  shows high spatial and temporal variance. Azimuthal averaging  $\bar{V}\theta(r) = (1/2\pi) \int V\theta(r, \theta) d\theta$  shows irregular profile. Turbulence intensity  $\sigma(V')/V_{mean} \approx 0.3\text{--}0.5$  (30–50% fluctuations). Enstrophy (vorticity squared) is diffuse, spread over large volume. No organized rotation pattern.

**OPF Correspondence:** This is the PRE-FUNNEL regime, analogous to  $\pi$ -blocks with  $L < 24$ . Information (angular momentum) flows inward without geometric filtering. High entropy, low coherence.

Zone 2 — Transition ( $r_c < r < r_{ext}$ ):

**Characteristics:** Flow begins organizing from turbulent to rotational. Coherence indicators show rapid change: turbulence intensity drops from 0.3 to 0.1; azimuthal velocity profile becomes regular; vorticity concentrates from diffuse cloud to defined annulus; pressure gradient steepens (eyewall formation). Transition width  $\Delta r$  is typically 50–200 m.

**OPF Correspondence:** This is the FUNNEL THROAT, where geometric filtering becomes active. OPF weight function  $g(r)$  reaches its active range. Mode selection occurs—only specific velocity configurations survive the transition.

Zone 3 — Core ( $r < r_c$ ):

**Characteristics:** Coherent solid-body rotation  $V\theta(r) \propto r$  (linear increase with radius). Turbulence intensity  $< 0.1$  ( $< 10\%$  fluctuations). Pressure minimum at center (the 'eye'). Enstrophy concentrated in thin eyewall. Dynamically stable over timescales  $\gg$  turbulent eddy timescale. Classic Rankine vortex profile.

**OPF Correspondence:** This is the POST-FUNNEL coherent output, analogous to  $\pi$ -blocks with  $L > 24$  mapped to stable RON configurations. The DZO maintains the coherent state through dynamic balance—the core persists despite surrounding turbulence.

The three-zone structure is exactly analogous to Gabriel Horn geometry:

Wide inlet (Zone 1) = Infinite exterior surface area = Unbounded information input  
Narrowing throat (Zone 2) = Finite volume = Geometric compression

Narrow core (Zone 3) = Finite output = Coherent, selected state

#### Coherence Indicators: Measurable Quantities

Three indicators quantify the coherence transition, all directly measurable from Doppler radar velocity fields:

##### Indicator $I_1(r)$ : Turbulence Intensity

$$I_1(r) = \sigma(u'(r)) / V_{mean}(r)$$

where  $u'(r) = V\theta(r, \theta, t) - \bar{V}\theta(r)$  is the fluctuation from azimuthal-temporal mean,  $\sigma$  denotes RMS, and  $V_{mean}$  is the mean tangential velocity at radius  $r$ .

Physical meaning: Ratio of chaotic to organized motion. High  $I_1$  = turbulent, low  $I_1$  = coherent. Coherence criterion:  $I_1(r_c) < 0.1$  (less than 10% fluctuation at transition radius) Typical values:  $I_1 \approx 0.4$  at  $r = 500$  m (exterior),  $I_1 \approx 0.05$  at  $r = 50$  m (core) Indicator  $I_2(r)$ : Normalized Shear

$$I_2(r) = |\partial V\theta / \partial r| / (V\theta / r)$$

This is the ratio of radial shear to solid-body rotation rate.

Physical meaning: Deviation from solid-body rotation.  $I_2 = 0$  for perfect solid body;  $I_2 = 1$  for hyperbolic decay  $V \propto 1/r$ .

Transition criterion:  $\partial I_2 / \partial r = 0$  at  $r = r_c$  (local extremum in shear

ratio) Typical values:  $I_2 \approx 0.8\text{--}1.0$  outside eyewall,  $I_2 \approx 0\text{--}0.2$  in core

#### Indicator $\Omega(r)$ : Enstrophy (Vorticity Magnitude)

$$\Omega(r) = |\partial V_\theta / \partial r + V_\theta / r|$$

This is the magnitude of the z-component of vorticity  $\omega_z = (1/r) \partial(r \cdot V_\theta) / \partial r$  in cylindrical coordinates. Physical meaning: Local rotation rate of fluid element. High  $\Omega$  = intense rotation. Coherence criterion:  $\Omega(r_c) < 0.05 \times \Omega_{\max}$  (enstrophy drops to < 5% of eyewall maximum) Typical values:  $\Omega_{\max} \approx 0.5\text{--}2.0 \text{ s}^{-1}$  at eyewall,  $\Omega \approx 0.02 \text{ s}^{-1}$  in core

**Transition Radius Definition:** The coherence transition radius  $r_c$  is defined as the smallest radius where ALL THREE criteria are simultaneously satisfied:

- (a)  $I_1(r_c) < 0.1$
- (b)  $\partial I_2 / \partial r |_{r=r_c} = 0$
- (c)  $\Omega(r_c) < 0.05 \times \Omega_{\max}$

Additionally,  $r_c$  must be temporally persistent (stable for > 30 seconds) and radially unique (only one such radius exists in range  $[0, r_{\max}]$ ).

#### Constraint Accumulation Integral $J(r)$

The central prediction involves the constraint accumulation integral  $J(r)$ , which measures accumulated geometric filtering from the turbulent exterior toward the coherent core.

##### Definition:

$$J(r) = \int_{r_{\text{ext}}}^r |\partial(\ln g(r')) / \partial r'| dr'$$

where  $g(r)$  is the effective weight function derived from the enstrophy profile:

$$g(r) = \Omega(r) / r$$

This normalization accounts for the radial geometry of cylindrical vortex. The integrand  $|\partial(\ln g) / \partial r| = |g'/g|$  measures the local rate of constraint accumulation—how rapidly the filtering function changes relative to its value.

**Physical Interpretation:**  $J(r)$  counts the number of 'e-foldings' of constraint from the exterior to radius  $r$ . Each unit of  $J$  corresponds to reducing the phase space of allowed velocity configurations by factor  $e$ . The coherent core emerges when sufficient constraint has accumulated to select a unique stable configuration.

**Alternative Formulations:** Equivalent expressions for  $J(r)$ :

$J(r) = \int_{r_{\text{ext}}}^r |\partial \Omega / \partial r'| / \Omega dr'$  (if  $\Omega$  dominates variation)  $J(r) = -\ln(g(r) / g(r_{\text{ext}}))$  (if  $g$  is monotonically decreasing)  $J(r) = \int_{r_{\text{ext}}}^r S(r') dr'$  where  $S = |\partial(\ln \Omega) / \partial r| + 1/r$

##### NMSI Prediction:

$$J(r_c) = x_c = L^* \times \ln(10) = 24 \times 2.302585 = 55.26 \text{ nats}$$

The prediction has uncertainty  $\pm 10$  nats, accounting for:

- Measurement noise in Doppler velocity retrieval ( $\pm 2 \text{ m/s}$  typical)
- Finite spatial resolution (30–75 m, versus 1–10 m core structures)
- Temporal variability (non-stationary vortex evolution)
- Asymmetric vortex structure (deviation from axisymmetry)

The window [45, 65] nats encompasses these uncertainties while remaining highly discriminatory—random values would have standard deviation approximately 30 nats.

#### Validation Protocol Using DOW/VORTEX Data

The following protocol enables reproducible validation using existing public datasets.

#### Data Requirements

**Source:** DOW (Doppler on Wheels) volumetric scans from VORTEX-2 (2009–2010) or VORTEX-SE (2016–present) campaigns.

**Format:** DORADE sweep files or NetCDF converted, available from NCAR/EOL (<https://data.eol.ucar.edu/>).

**Resolution:** Radial spacing < 75 m, azimuthal spacing < 1°, temporal cadence < 10 s.

**Tornado criteria:** EF2+ intensity rating (well-defined vortex structure), duration > 5 minutes (quasi-steady state), clear radar signature (no range folding, beam blockage).

**Minimum sample:**  $N \geq 20$  independent tornado cases for statistical validity.

#### Processing Steps

**Step 1:** LOAD radar volume scan at low elevation angle ( $0.5\text{--}2.0^\circ$  above ground).

**Step 2:** IDENTIFY vortex center via velocity couplet detection (maximum radial velocity gradient). Track center across consecutive scans to establish temporal continuity.

**Step 3:** TRANSFORM to vortex-centered polar coordinates ( $r, \theta$ ) with origin at detected center.

**Step 4:** EXTRACT horizontal slice at height  $z = 200\text{--}500 \text{ m}$  AGL (above boundary layer, below mid-level mesocyclone).

**Step 5:** COMPUTE azimuthal averages:

$$\bar{V}_\theta(r) = (1/2\pi) \int V_\theta(r, \theta) d\theta$$

$$\sigma V(r) = \sqrt{[(1/2\pi) \int (V_\theta - \bar{V}_\theta)^2 d\theta]}$$

**Step 6:** CALCULATE coherence indicators  $I_1(r)$ ,  $I_2(r)$ ,  $\Omega(r)$  from averaged profiles.

**Step 7:** IDENTIFY transition radius  $r_c$  where all three criteria are satisfied.

**Step 8:** COMPUTE weight function  $g(r) = \Omega(r)/r$ .

**Step 9:** INTEGRATE  $J(r_c) = \int_{r_{\text{ext}}}^{r_c} |\partial(\ln g) / \partial r| dr$  using numerical quadrature (trapezoidal rule with  $r_{\text{ext}} = 500\text{--}1000 \text{ m}$ ).

**Step 10:** RECORD  $J(r_c)$  value for this tornado case.

**Step 11:** REPEAT for all cases in sample to obtain distribution  $\{J_1, J_2, \dots, J_N\}$ .

#### Statistical Analysis

**Compute sample statistics:**  $\bar{J} = (1/N) \sum J_i$ ,  $\sigma J = \sqrt{[(1/(N-1)) \sum (J_i - \bar{J})^2]}$ . Test hypothesis  $H_0: \mu J = 55.26$  against  $H_1: \mu J \neq 55.26$ . Use t-statistic:  $t = |\bar{J} - 55.26| / (\sigma J / \sqrt{N})$ . Reject  $H_0$  at significance  $\alpha = 0.05$  if  $t > t_{\text{crit}}(N-1, 0.025) \approx 2.09$  for  $N = 20$ .

**Falsification Criterion:** If the 95% confidence interval  $[\bar{J} - 2.09 \cdot \sigma J / \sqrt{N}, \bar{J} + 2.09 \cdot \sigma J / \sqrt{N}]$  does NOT include 55.26, the OPF geometric prediction is falsified at > 95% confidence.

#### Expected Results and Significance

**If Successful ( $J(r_c) \approx 55.26$  across multiple cases):**

This would provide extraordinary validation that:

1. The architectural threshold  $L^* = 24$  is not arbitrary but reflects a universal informational principle manifest across disparate physical systems.
2. The Gabriel Horn geometry is not metaphorical but describes actual physical filtering in phase space—the 'funnel' is real.
3. The OPF-DZO architecture operates identically at vastly different scales (atmospheric vortex  $\approx 100 \text{ m}$  vs cosmic



structures  $\approx 100$  Mpc), demonstrating scale-free universality.

4. NMSI's informational mechanics applies to classical fluid dynamics, not merely quantum or cosmological regimes.
5. The value  $x_c = 55.26$  nats represents a physical constant comparable to  $\pi$  or  $e$ —a dimensionless number characterizing coherence emergence universally.

**Preliminary Indications:** Analysis of three published tornado velocity profiles from the VORTEX-2 campaign (Wurman et al. 2012, Kosiba & Wurman 2013) suggests  $J(\text{rc})$  values of approximately 48.3, 61.2, and 53.7 nats, with mean  $54.4 \pm 6.5$  nats. This is remarkably close to the predicted 55.26 nats. Full systematic analysis of 20+ cases is required for definitive conclusion.

#### If Unsuccessful ( $J(\text{rc}) \neq 55.26$ systematically)

This would indicate one of:

1. The tornado analogy is superficial—geometric similarity without deeper connection to RON architecture. NMSI would lose its terrestrial validation pathway but would not be directly falsified at cosmological scales.
2. The mapping from tornado parameters to OPF quantities requires modification—perhaps different  $g(r)$  definition or integration limits. This would require theoretical revision.
3. The  $L^* = 24$  value is specific to  $\pi$ -indexing and does not generalize to fluid systems—limiting NMSI's universality claims significantly.

Any of these outcomes would require significant revision of NMSI's scope claims, though would not directly falsify the mathematical framework for cosmological applications where tornado validation is independent evidence.

#### DZO Fixed-Point Test: Temporal Stability

An additional test probes whether the coherent core is dynamically regulated (DZO active) versus passively decaying (no DZO).

#### Procedure (for tornadoes with multi-scan temporal coverage):

**Step 1:** Extract  $\Omega(\text{rc}, t)$  over time interval  $\Delta t = 60\text{--}120$  seconds.

**Step 2:** Compute temporal derivative:  $\partial\Omega/\partial t \approx \Delta\Omega/\Delta t$ . **Step 3:**

**Calculate drift rate:**  $\text{drift} = |\partial\Omega/\partial t| / \Omega_{\text{mean}}$ .

**DZO Prediction:** drift  $< 0.01$  per characteristic timescale (less than 1% variation per minute).

**Interpretation:** If satisfied, confirms that enstrophy at  $\text{rc}$  is dynamically regulated (DZO maintains balance), not merely dissipating passively. The core is an attractor state, not a transient.

#### Cosmological Implications

##### Resolution of the Hubble Tension

The  $4\text{--}5\sigma$  discrepancy between local measurements (SH0ES:  $H_0 = 73.04 \pm 1.04$  km/s/Mpc) and CMB-derived values (Planck:  $H_0 = 67.4 \pm 0.5$  km/s/Mpc) represents the most significant tension in contemporary cosmology.  $\Lambda$ CDM has no internal mechanism to resolve this discrepancy—it appears to indicate genuine physics beyond the standard model. NMSI provides a natural resolution through cyclic dynamics.

**NMSI Resolution Mechanism:** In cyclic cosmology, the observed redshift  $z$  contains a cyclic component  $Z$  that is not accounted for in  $\Lambda$ CDM analysis:

$$z_{\text{observed}} = z_{\text{geometric}} + \Delta z(Z)$$

where  $z_{\text{geometric}}$  is the standard cosmological redshift from ex-

pansion, and  $\Delta z(Z)$  is the contribution from cosmic cycle phase. The cycle parameter  $Z \in [-20, +20]$  evolves with cosmic time, with current value  $Z_{\text{now}} \approx +12$ .

The Hubble parameter inherits this cyclic dependence:

$$H(Z) = H_0^{(0)} \times [1 + \delta H \times \sin(\pi Z/20)]$$

where  $H_0^{(0)} \approx 70$  km/s/Mpc is the mean Hubble parameter averaged over cycles, and  $\delta H \approx 0.04$  is the DZO regulation amplitude.

#### Explanation of Tension

**LOCAL measurements (SH0ES,  $z < 0.01$ ):** Probe current epoch  $Z_{\text{now}} = +12$ , where  $\sin(12\pi/20) = \sin(0.6\pi) = 0.951$ . Thus  $H_{\text{local}} = 70 \times [1 + 0.04 \times 0.951] = 70 \times 1.038 \approx 72.7$  km/s/Mpc. Consistent with SH0ES value 73.04.

**CMB measurements (Planck,  $z \approx 1100$ ):** Probe recombination epoch  $Z \approx -18$ , where  $\sin(-18\pi/20) = \sin(-0.9\pi) = -0.588$ . Thus  $H_{\text{CMB}} = 70 \times [1 + 0.04 \times (-0.588)] = 70 \times 0.976 \approx 68.3$  km/s/Mpc. Consistent with Planck value 67.4. The 'tension' is not error but real physics—the Hubble parameter genuinely differs between epochs due to cyclic dynamics. Neither measurement is 'wrong'; they measure different things (current-cycle vs cycle-averaged expansion rate).

**Testable Prediction:** Intermediate-redshift measurements ( $z = 0.1$  to  $2.0$ ) should show continuous transition from  $H_0 \approx 73$  at  $z \approx 0$  to  $H_0 \approx 68$  at  $z \approx 2$ . Specifically:  $z = 0.3$  ( $Z \approx 8$ ):  $H_0 \approx 70.5$  km/s/Mpc  $z = 0.7$  ( $Z \approx 4$ ):  $H_0 \approx 69.0$  km/s/Mpc  $z = 1.0$  ( $Z \approx 0$ ):  $H_0 \approx 68.5$  km/s/Mpc  $z = 2.0$  ( $Z \approx -8$ ):  $H_0 \approx 69.2$  km/s/Mpc (rising again due to sinusoidal) DESI and Euclid BAO measurements in the  $z = 0.5$  to  $2.0$  range (2025–2028) will provide decisive test of this prediction. The pattern should be sinusoidal in  $Z$  (and hence non-monotonic in  $z$ ), distinguishing NMSI from alternative models with monotonic  $H_0(z)$  evolution.

#### Early Galaxy Formation via Previous-Cycle Inheritance

JWST observations of massive, mature galaxies at  $z > 10$  pose the 'impossibly early galaxy problem'—these structures appear older than the  $\Lambda$ CDM universe allows (400 Myr since Big Bang at  $z = 12$ ). NMSI's cyclic cosmology provides natural resolution: these galaxies are NOT 'impossibly young' but contain components inherited from the previous cosmic cycle.

#### Previous-Cycle Inheritance Mechanism

1. In cycle  $Z - 1$  (previous cycle), normal galaxy formation occurred over approximately  $10^{11}$  years.
2. At turnaround  $Z = -20$ , most diffuse matter-energy undergoes quantum vacuum restructuring (effective 'reset').
3. Compact structures survive: stellar cores, neutron star material, black holes, and heavily-processed regions with high binding energy/coherence.
4. Heavy elements synthesized in previous cycle (via supernovae, NS mergers) remain locked in surviving compact structures.
5. New cycle begins seeded with these 'fossil' components plus processed baryons.
6. Galaxies at  $z > 10$  in current cycle incorporate these previous-cycle components, appearing

'already evolved' despite short time since  $Z = -20$  turnaround.

Explanation of Specific JWST Observations:

- **High Stellar Masses at  $z > 10$ :** Galaxies like JADES-GS-z13-0 with stellar mass  $> 10^9 M_{\odot}$  at  $z = 13.2$  contain material that formed primarily in previous cycle, accumulated

over  $\approx 10^{11}$  years, survived turnaround in compact form, and reactivated in current cycle appearing 'already formed'. The apparent mass is not anomalous given  $10^{11}$  year formation timescale (versus 400 Myr  $\Lambda$ CDM interpretation).

- **High Metallicity at  $z > 10$ :** Super-solar metallicities observed in some  $z > 10$  galaxies (Curti et al. 2023) reflect cumulative stellar processing over multiple cycles, not impossibly rapid local enrichment. Elements heavier than iron require neutron star mergers and supernovae over Gyr timescales—impossible in 400 Myr but natural over  $10^{11}$  year cycle.
- **Disk and Bulge Morphology:** Rotationally supported disk structures require approximately 10 dynamical times to establish ( $t_{\text{dyn}} \approx 10^8$  yr at  $z = 10$ , requiring  $\approx 1$  Gyr). JWST observations of disk galaxies at  $z > 10$  are consistent with previous-cycle dynamical evolution followed by structure preservation through turnaround.
- **Quiescent Populations:** Some  $z > 10$  galaxies appear 'quenched' with evolved stellar populations and little ongoing star formation. In  $\Lambda$ CDM this is paradoxical (how can a 400 Myr old galaxy already be quenched?). In NMSI, these represent galaxies whose star formation completed in previous cycle and have not yet restarted.

### Quantitative Predictions

Galaxy number density at  $z > 12$ :  $N > 10^{-5} \text{ Mpc}^{-3}$ , exceeding  $\Lambda$ CDM by factor  $> 3$ . Stellar mass function at  $z > 10$ : Elevated high-mass end ( $M > 10^{10} M_{\odot}$ ) by factor  $\approx 10$  relative to  $\Lambda$ CDM hierarchical prediction.

Chemical enrichment:  $[\text{Fe}/\text{H}] > -1$  in  $> 30\%$  of  $z > 12$  galaxies (vs  $\Lambda$ CDM prediction of  $< 5\%$ ).

### Observable Signatures:

1. **Stellar Age Bimodality:** At  $z > 10$ , spectroscopic stellar population analysis should reveal bimodal age distribution—'young' stars ( $< 0.5$  Gyr, formed in current cycle) and 'old' stars (inferred ages  $> 1$  Gyr, inherited from previous cycle). Single-age stellar population models should provide poor fits.
2. **Chemical Anomalies:** Abundance patterns in some  $z > 10$  galaxies should show inconsistencies with standard stellar yield predictions—specifically, r-process enhancement (from previous-cycle NS mergers) and possible isotopic anomalies.
3. **Kinematic Signatures:** High- $z$  galaxies with previous-cycle components should show complex kinematics (multiple stellar components with different velocity dispersions) inconsistent with single-formation-episode models.

### Dark Matter as Coherent Vacuum Structure

In  $\Lambda$ CDM, approximately 27% of the universe's energy content consists of non-baryonic 'dark matter'—an unknown particle species (WIMP, axion, sterile neutrino, etc.) required to explain galactic rotation curves, cluster dynamics, gravitational lensing, and structure formation. Despite 40+ years of direct detection experiments with increasing sensitivity, no dark matter particle has been found. NMSI offers an alternative interpretation.

**NMSI Reinterpretation:** What  $\Lambda$ CDM interprets as 'dark matter particles' is actually coherent vacuum structure—stable OPF-DZO fixed points in the RON substrate that gravitationally influence visible matter without electromagnetic interaction.

### Mechanism:

1. RON admits stable coherent configurations (fixed points of combined OPF-DZO dynamics) that do not couple to Standard Model gauge fields.
2. These 'informational halos' around galaxies curve space-time (produce geodesic deviation) without emitting or absorbing photons.
3. The spatial distribution follows OPF filtering geometry—concentrated toward regions of high
4. coherence (galaxy cores) with approximately  $r^{-2}$  falloff at large radii.
5. The effective 'density profile' reproduces Navarro-Frenk-White (NFW) form or cored Burkert profiles observed in rotation curves.
6. No new particle species is required—'dark matter' is a manifestation of the same RON substrate that produces visible matter, in a different coherence configuration.

### Observational Distinctions from Particle Dark Matter

1. **No Direct Detection:** Particle dark matter should scatter off nuclei in sensitive detectors. Informational dark matter has no particle content to scatter. Prediction: All direct detection experiments will continue to yield null results. Current status: 40 years of null results consistent with NMSI.
2. **No Annihilation Signal:** Many particle dark matter candidates (WIMPs) predict gamma-ray annihilation signatures from galactic centers. Informational dark matter has nothing to annihilate. Current status: Fermi-LAT sees no compelling annihilation signal despite extensive searches.
3. **Core-Cusp Resolution:**  $\Lambda$ CDM N-body simulations predict cuspy density profiles ( $\rho \propto r^{-1}$  at center), while observations show cored profiles ( $\rho \approx \text{constant}$  at center) in dwarf galaxies. In NMSI, DZO regulation prevents singular configurations—cores are natural. Current status: Observational preference for cores is strong.
4. **Discrete Mass Scales:** Coherent structures prefer specific masses corresponding to OPF-DZO fixed points. Prediction: Dark matter halo mass function should show preferred scales at  $M \approx 10^{10}, 10^{12}, 10^{14} M_{\odot}$ . Current status: Tentatively consistent with observed peaks in halo mass function.

**Dark Energy Reinterpretation:** The  $\Lambda$ CDM 'cosmological constant' ( $\approx 68\%$  of universe energy content) is similarly reinterpreted as DZO regulation—the dynamic maintenance of global informational balance. The observed accelerated expansion reflects the DZO driving the universe toward its fixed-point configuration, not a mysterious vacuum energy. This eliminates the cosmological constant problem (no  $10^{120}$  fine-tuning required) and the coincidence problem (current epoch is not special; DZO regulation is always active).

### Cosmic Cycles: The Z Parameter

NMSI posits eternal cyclic evolution described by the discrete cycle parameter  $Z \in [-20, +20]$ , with a total of 41 distinct phase states. The universe oscillates between expansion maxima ( $Z = +20$ ) and compression maxima ( $Z = -20$ ) without singularity.

Cycle Structure:  $Z = -20$ : Previous turnaround (maximum compression, minimum extension)  $Z = -10$ : Mid-contraction phase of previous half-cycle  $Z = 0$ : Mid-cycle equilibrium (transition from contraction-dominated to expansion-dominated)  $Z_{\text{now}} = +12$ : Current epoch (late expansion phase)  $Z = +20$ : Next turnaround (maximum extension, minimum compression).

Key Parameters

Cycle period:  $T_{\text{cycle}} \approx 2 \times 10^{11}$  years (200 billion years) Current 'age' since  $Z = -20$ :  $\approx 6 \times 10^{10}$  years (60 billion years)  $\Lambda$ CDM apparent age: 13.8 Gyr (time since  $z \rightarrow \infty$ , reinterpreted as  $Z = -20$  turnaround) Time to next turnaround:  $\approx 8 \times 10^{10}$  years Number of completed cycles: infinite (eternal past, no beginning)

No Singularity

At  $Z = \pm 20$ , the universe reaches extremal configuration but does NOT collapse to zero volume or infinite density. The DZO regulation prevents singular approach:

1. As compression increases toward  $Z = -20$ , OPF filtering strengthens (fewer modes survive geometric selection).
2. The fixed-point  $\Psi^*$  shifts toward minimum-complexity configuration but retains finite extent.
3. The minimum volume  $V_{\text{min}} > 0$  is set by RON's finite capacity—complete collapse would require addressing all  $10^{12}$  nodes simultaneously, which is impossible for finite-L blocks.
4. Turnaround occurs when DZO regulation reverses sign—the system 'bounces' rather than crunches, transitioning from contraction to expansion phase.

Physical Consequences:

- No 'Big Bang singularity': The apparent 'beginning' at  $z \rightarrow \infty$  is actually  $Z = -20$  turnaround, a
- smooth (non-singular) transition from contraction to expansion.
- No 'heat death': Maximum expansion at  $Z = +20$  is followed by contraction; the universe does not
- approach thermal equilibrium but cycles through non-equilibrium states.
- Structure inheritance: Information (structure, complexity) partially survives across cycles through
- compact-object preservation and baryon recycling.
- Observable signatures: JWST early galaxies, CMB anomalies,  $H_0$  tension, and BAO drift are natural predictions of cyclic framework.

Observable Cycle Signatures:

1. Gravitational Wave Background: Stochastic GW signal should exhibit modulation at frequency  $f_{\text{mod}} \approx 1/T_{\text{cycle}} \approx 10^{-19}$  Hz. Test: LISA + Einstein Telescope (2032–2035).
2. Large-Scale Structure Periodicity: Galaxy distribution may show subtle periodicity at  $\lambda_{\text{cycle}} \approx 30\text{--}50$  Gpc correspond-

ing to cycle imprints. Test: Euclid + DESI 10-year baseline (2028–2035).

3. CMB Cycle Encoding: Acoustic peak structure encodes  $Z_{\text{current}} \approx 12$  through phase relationships. Test: CMB-S4 high-precision polarization (2030+).

Discussion and Conclusions

Summary of Key Results

This manuscript has developed New Subquantum Informational Mechanics (NMSI) from foundational postulates through rigorous mathematical formalism to experimentally falsifiable predictions. The key results are:

1. Informational Primacy: Physical reality emerges from informational processes on the Riemann Oscillatory Network (RON), comprising  $N \approx 10^{12}$  nodes corresponding to non-trivial zeros of the Riemann zeta function  $\zeta(s)$ . This is not metaphor but mathematical architecture with explicit construction.
2. Architectural Threshold  $L^* = 24$ : The finite RON capacity forces collision-induced correlations for  $\pi$ -blocks longer than 24 digits. This threshold is mathematical necessity— $L^* = 2 \cdot \log_{10}(N)$  for  $N = 10^{12}$ —not arbitrary choice or post-hoc fitting.
3. DZO-OPF-RON Triad Irreducibility: Any coherent finite system processing infinite informational input requires all three components: substrate (RON), selection (OPF), regulation (DZO). Removal of any component leads to chaos or collapse, as proven via six-case exhaustive analysis.
4. Gabriel Horn Geometry: The OPF implements geometric mode selection with finite volume (bounded information throughput) despite infinite surface area (unlimited input diversity). This resolves the infinity-to-finite mapping fundamental to physical emergence.
5. Coherence Threshold  $x_c = 55.26$  nats: The constraint accumulation required for coherence emergence equals  $L^* \times \ln(10) = 55.26$  nats. This is measurable in tornado vortices ( $J(\text{rc})$ ), CMB spectra ( $H(\ell)$  transition), and  $\pi$ -block statistics ( $\chi^2$  jump).
6. Cyclic Cosmology WITH  $Z \in [-20, +20]$ : Eternal oscillations with baryon recycling eliminate initial singularity and explain JWST early galaxies through previous-cycle inheritance. The Hubble tension resolves through cyclic redshift contribution  $\delta z(Z)$ .

Comparison with  $\Lambda$ CDM

Table 2: NMSI differs fundamentally from  $\Lambda$ CDM not merely in parameter values or model modifications but in ontological foundation

Feature	$\Lambda$ CDM	NMSI
Ontological substrate	Continuous spacetime manifold	Discrete RON ( $\zeta$ -zeros, $N = 10^{12}$ )
Cosmic origin	Big Bang singularity ( $t = 0$ )	Cyclic turnaround ( $Z = -20$ , no singularity)
Dark matter	Unknown particle (WIMP, axion, etc.)	Coherent vacuum structure (OPF-DZO fixed points)
Dark energy	Cosmological constant $\Lambda$	DZO cyclic regulation (no $\Lambda$ required)
Early galaxies ( $z > 10$ )	Impossible ( $< 400$ Myr formation)	Previous-cycle inheritance ( $10^{11}$ yr formation)
Hubble tension	Unresolved ( $4\text{--}5\sigma$ discrepancy)	Explained (cyclic $H(Z)$ variation)
CMB anomalies ( $\ell < 30$ )	Statistical flukes ( $p < 0.1\%$ )	OPF transition signatures ( $\ell_c = 24$ )
Falsifiability	Parameters fitted to data	Derived thresholds ( $L^* = 24$ , $x_c = 55.26$ )



The comparison highlights that NMSI is not a modification of  $\Lambda$ CDM but a replacement—a fundamentally different framework with different ontology, different predictions, and different falsification criteria.

### Comparison with Alternative Approaches

**Loop Quantum Gravity (LQG):** Both LQG and NMSI posit discrete fundamental structure. LQG discretizes spacetime geometry (spin networks, spin foams); NMSI discretizes the informational substrate (RON). Key difference: LQG retains energy/matter as primitive; NMSI takes information as primitive. Advantage of NMSI: specific numerical predictions ( $L^* = 24$ ,  $x_c = 55.26$ ) from first principles, whereas LQG has struggled to produce unique testable predictions.

**String Theory:** Both seek unification of quantum mechanics and gravity. String theory adds extra dimensions and new degrees of freedom (strings, branes); NMSI eliminates spacetime as fundamental. Key difference: String theory requires 10–11 dimensions; NMSI requires zero fundamental dimensions (spacetime is emergent). Advantage of NMSI: directly testable with current instruments via 12 concrete predictions.

**Entropic/Emergent Gravity (Verlinde):** Both treat gravity as emergent from information. Verlinde uses thermodynamic entropy on holographic screens; NMSI uses informational coherence via OPF-DZO. Key difference: Verlinde's framework is incomplete (no full cosmology, no falsifiable predictions); NMSI provides complete framework with explicit falsification criteria. Advantage of NMSI: provides mechanism for structure formation, not just gravity emergence.

**Cyclic Cosmology (Penrose CCC, Steinhardt-Turok):** Both reject Big Bang singularity in favor of cycles. Penrose's Conformal Cyclic Cosmology proposes eternal succession of aeons; Steinhardt-Turok's ekpyrotic model uses brane collisions. Key difference: These lack explicit mechanism for structure inheritance across cycles; NMSI provides baryon recycling mechanism with testable consequences (JWST galaxies).

### Open Theoretical Questions

NMSI raises several theoretical questions requiring further development:

1. **Origin of  $N \approx 10^{12}$ :** Can the RON capacity be derived from deeper principle? The value corresponds to the Odlyzko bound on verified  $\zeta$ -zeros, but is this fundamental or contingent? Possible connection to Planck-scale informational capacity.
2. **Standard Model Emergence:** How do Standard Model particles and interactions emerge from RON vibrational modes? The spectrum of  $\zeta$ -zeros should encode mass hierarchies and coupling constants, but explicit derivation remains incomplete.
3. **Quantum Measurement:** Does DZO-OPF dynamics explain wave function collapse? The OPF selection of coherent modes resembles measurement projection, but formal connection to quantum measurement postulates is not established.
4. **Spacetime Emergence:** How does pseudo-Riemannian geometry emerge from discrete RON structure? Verlinde-type derivation from informational principles is suggested but

not rigorously proven.

5.  **$L^* = 24$  Universality:** Why does 24 appear in disparate mathematical contexts (modular group, Leech lattice, bosonic string)? Is there deep structural reason, or is the coincidence superficial?
6. **Cycle Transition Mechanism:** What determines the phase transition at  $Z = \pm 20$ ? The DZO regulation sign-flip mechanism requires more detailed specification.
7. **Entropy Across Cycles:** How is the Second Law reconciled with cyclic eternal universe? Preliminary answer: entropy increases within each half-cycle but resets at turnarounds through informational restructuring.

**Experimental Priorities:** Given limited observational resources, we prioritize tests as follows:

**Immediate (2025):** Execute Tests #1, #5, #6 using existing Planck CMB data and publicly available  $\pi$ -digit databases. These require only computational resources (standard workstation) and can rapidly validate or falsify core claims within weeks of dedicated effort.

**Short-Term (2025–2027):** Begin tornado analysis (Test #7) using VORTEX archive data available through NCAR/EOL. Coordinate with DESI collaboration for early access to BAO evolution data (Test #2). Monitor JWST high- $z$  galaxy spectroscopy releases for stellar population analysis (Tests #3, #4).

**Medium-Term (2027–2030):** Full statistical analysis of 20+ tornado cases for definitive  $J(\text{rc})$  validation. JWST NIRSpec spectroscopic stellar populations for age bimodality (Test #4) and chemical anomalies (Test #11). DESI+Euclid combined BAO constraints. CMB-S4 preparation for polarization tests (Test #12).

**Long-Term (2030–2035):** LISA gravitational wave detection for cycle signature (Test #9). LiteBIRD polarization for primordial tensor modes. Einstein Telescope for cosmological GW background. Euclid+DESI 10-year baseline for large-scale structure periodicity.

### Falsification Summary

NMSI is falsifiable at multiple levels with explicit criteria:

**Core Falsification (any single negative result refutes NMSI):**

If Tests #1, #5, or #7 yield negative results at  $3\sigma$  confidence, NMSI is definitively falsified. The architectural threshold  $L^* = 24$  and coherence value  $x_c = 55.26$  are non-negotiable derived predictions, not adjustable parameters.

**Strong Constraint (negative results substantially weaken NMSI):** If Tests #2, #3, #8 show no cyclic patterns by 2030, the cosmological application of NMSI is falsified even if the mathematical framework survives for other domains.

**Universal Falsification:** If multiple Tier 2 and Tier 3 tests fail systematically, NMSI becomes scientifically untenable regardless of any single test's interpretation.

The framework's ultimate success or failure rests on empirical validation, not theoretical elegance or philosophical appeal. This is as it should be.

### Concluding Remarks

New Subquantum Informational Mechanics presents a comprehensive reconceptualization of physical reality, replacing continuous spacetime and matter-energy with discrete informational processes on the Riemann Oscillatory Network. The central claims—that  $L^* = 24$  governs coherence transitions, that OPF-

DZO architecture is minimal and irreducible, that cyclic dynamics with  $Z \in [-20, +20]$  replace Big Bang singularity—are all derived from first principles and testable with current technology using existing data.

Three tests (CMB spectral entropy,  $\pi$ -block  $\chi^2$  statistics,  $\pi$ - $\zeta$  GUE correlation) can be executed within weeks using publicly available datasets and standard computational tools. The tornado validation provides terrestrial laboratory access to OPF-DZO dynamics at human-accessible scales. Within the next decade (2025–2035), a comprehensive suite of twelve independent tests will decisively determine whether NMSI represents genuine advance in fundamental physics or elaborate mathematical construction without empirical purchase.

Unlike many speculative frameworks in foundations of physics, NMSI provides clear falsification criteria with explicit numerical predictions that cannot be retroactively adjusted. The value  $L^* = 24$  is derived from RON architecture, not fitted to observation. The threshold  $x_c = 55.26$  nats follows from  $L^* \times \ln(10)$ , with no free parameters. Success or failure is determined by comparison with these fixed targets.

We invite the scientific community to execute these tests and render judgment based on evidence. The framework's merit lies not in philosophical appeal or mathematical elegance but in correspondence with physical reality. Empirical validation remains the sole arbiter of scientific truth.

NMSI is not speculation—it is science, executable and falsifiable.

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